

Longitudinal Analysis of Salary Discrimination in Higher Education

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Abstract

Legal and statistical issues associated with the use of multiple regression models in faculty discrimination cases in higher education are presented in this paper. Faculty salary models as a function of gender, rank, tenure status, race, academic discipline, and age variables are analyzed in a longitudinal study covering three years (1982-84) at the University of Northern Colorado (UNC). Declining student enrollment during the period saw the size of the faculty drop from a high of 492 in 1982 to a low of 380 in 1984. Results of the exploratory data analysis indicate declining roles for gender, race and age variables in explaining salary differences. While the contribution of academic discipline variables in the regression models was statistically significant, results seem consistent with institutional salary policies which were in effect at each point in time.

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Introduction

Given the increasing frequency of litigation on matters of discrimination with regard to salaries in higher education, the courts are faced with statistical evidence that support and refute claims of discrimination at an ever increasing magnitude and complexity. The claims of discrimination are made on the basis of race, gender and age factors.

Within the past ten years, multiple regression techniques have become popular in litigation on discrimination. Two recent articles support the use of multiple regression techniques in judicial studies of race and sex discrimination, (Finkelstein, 1980; Fisher, 1980). Both researchers identify several concerns which must be addressed.

Finkelstein discusses the problems associated with the use of "tainted" variables. Predictor variables specified to reflect productivity are often affected by discriminatory practice themselves. For example, when using the variables of tenure status and rank to predict salaries, discrimination might also be present in tenure and promotion decisions (Finkelstein, 1980), thus the inclusion of the "tainted" variables may serve to mask salary discrimination if it exists.

Fisher (1980) discusses the assumptions underlying multiple regression analysis and points out the problems associated with multicollinearity and the "shotgun" approach to analyze the data. Too often, the analysis is performed with an overprescription of

independent variables in an attempt to discover what may be related to the criterion variable. When many variables are included, the risk of multicollinearity is increased. As a result, the magnitude and even the sign of the coefficients in the model may be affected. Fisher warns against the "shotgun" approach. He advises the experimenter to select carefully the variables to be used and develop a rationale for inclusion which can be defended.

Recently, studies have appeared which use other statistical techniques such as canonical correlation and multiple discriminant analysis, Carter, et al. (1983). Carter applies these techniques to analyze salary equity at the University of Wisconsin at Superior for two successive years, 1981-82 and 1982-83.

The two techniques used by Carter provide an alternative to address some of the concerns expressed by Finkelstein with regard to violation of assumptions in the multiple linear regression models. Specifically, the concern about "tainted" variables can be addressed by using canonical correlation and multiple discriminant analysis. These techniques assist the experimenter in determining whether or not the variables of tenure status and rank are affected by the variables of race, age or gender. If this analysis confirms the variables in question are not "tainted", then the multiple regression model can make use of the variables to improve the fit. If, however, the analysis reveals the variables are "tainted", the regression model will exclude

those variables in the model. In addition, the very fact that the variables are discovered to be tainted is important information which may be used to resolve discriminatory practices.

All three statistical procedures, multiple regression, canonical correlation, and discriminant analysis, are used in this longitudinal study of salary practices at the University of Northern Colorado (UNC). Data on all full-time faculty members at UNC for the academic years 1982-83, 1983-84, and 1984-85 are analyzed to determine the existence of salary discrimination on the basis of race, age or sex. The items collected on each faculty member include: salary, rank, tenure status, highest degree, years employed at UNC, years in each rank, years at UNC before obtaining tenure, years with the doctorate, discipline, sex, race and age.

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The longitudinal data allows for an analysis of changes in salary practices as they are affected by changes in University policies. This paper relates University policy changes which occurred during the three-year period to the changes in the existence and/or extent of discrimination in UNC salaries.

The paper is subdivided into four major sections: multiple regression analysis of salaries for the three years, canonical correlation on rank and tenure status versus qualification, experience and discrimination variables, multiple discriminant analysis to determine classifications and misclassifications with regard to rank and tenure status, and a contextual analysis which

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compares the UNC policy changes to the state of salary patterns at UNC during the three-year period.

Variables included in the statistical analyses of salary discrimination at UNC for the years 1982-83 through 1984-85 are presented in Table 1. Before proceeding with the statistical analyses several precautions were taken to insure the internal validity of the study. First, patterns of discrimination among the predictor variables themselves were examined using discriminant analysis and canonical correlation techniques. That is to say, relationships between university status variables (e.g., tenure status, rank, rate of promotion) and the discrimination variables were carefully examined before they were included in the regression models as predictor variables. If university status variables are tainted they should be removed. Second, collinearity diagnostics were obtained on the predictor variables. Although our primary interest is in the use of $\ensuremath{\text{R}^2}$ values, interpretation of the regression coefficients themselves is also of interest. It can be shown that the presence of collinearity can affect both the sign and magnitude of the regression coefficients (Pedhazur, 1982). Detection of collinearity among the predictor variables would require us to re-think the specification of our model:

Inspection of the collinearity diagnostics from the regression procedure of the Statistical Analysis System (1982)

indicated that the variables Longevity and Years with Doctorate were the primary sources of collinearity. Inasmuch as these variables were selected to contribute unique information to the model, the preliminary analyses indicate that these variables were already adequately represented by other predictors. Our solution to the problem was to delete Longevity and Years with the Doctorate from the set of predictor variables.

In the sections that follow, results form the canonical correlation and discriminant analyses designed to detect patterns of discrimination among the set of predictor variables are reported.

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Canonical Correlation Analysis

In an attempt to ferret out potential patterns of discrimination during the past three academic years at UNC, canonical correlational analytic methods were undertaken. Canonical Analysis (CA) is a method designed to study the relations between two sets of variables, a set of predictor variables and a set of criterion variables. The set of independent or predictor variables (PV) identified in this study consisted of all the discrimination variables which included gender, race, and age. On the other hand, the set of dependent or criterion variables (CV) could be classified as university status

Table 1
Variables Included in the Analysis of Salary Discrimination

Variable	Description	
	Rank	
٧1	Assistant Professor	
٧2	Associate Professor	
V2	Professor	
	Longevity	
٧4	Years of Service	
	Degree	
٧5	Master's	•
٧6	Doctorate	
	Tenure Status	
٧7	Yes=1, No=0	
	Gender	
٧8	Male=l, Female=O	
	Race	
٧9	Caucasian=1, Otherwise=0	
V11	Black=1. Otherwise=0	
V12	Hispanic=1, Otherwise=0	
	Else, Oriental, or Indian	
	Time in Rank	
V14	Years as Instructor	
V15	Years as Assistant Professor	
V16	Years as Associate Professor	
V16 V17	Years as Professor	
	Time Since Receiving Doctorate	
V18	Years with the Doctorate	
	Time Before Receiving Tenure	
V1 9	Years before Receiving Tenure	
	Discipline	
V20	School of Business=1, Otherwise=0	
V21	Physical Sciences=1, Otherwise=0	
V22	Social Sciences=1, Otherwise=0	
V23	Humanities=1, Otherwise=0	
V24	College of Performing & Visual Arts=1, Otherwise=0	
V25	College of Health and Human Services=1, Otherwise=0	
	Else. College of Education .	
V29	Age	
Ÿ30	Salary	

variables. These variables included tenure, academic rank, degree earned, years spent at each level, and school or college in which the faculty member was assigned. The set of discrimination or predictor variables numbered six whereas there were 17 university status or criterion variables. Thus, the maximum number of linear combinations or composites of predictor variables and criterion variables which could be tested for a significant correlation is six.

Each of the possible six canonical correlations (Canonical R) for each of the three academic year studied at UNC was tested for statistical significance by converting Wilks' Lambda to an approximate F. In Table 2 are presented the standardized weights for the set of predictors and set of criteria associated with the three significant canonical R-values using N = 492 observations of the 1982-83 study group. All three canonical R-values are significant beyond the 0.001 level and the three canonical R-values in descending order are .76, .42, and .38. The remaining three non-significant canonical R-values and corresponding standardized weights are not reported.

The results for the 1983-84 study are presented in Table 3. It should be observed that only two of the canonical R-values were statistically significant for N=446 observations used in the

1e 2 onical Solution Using Standardized Weights for Significant Relationships for N = 492 ervations (1982-83)

dictor iables	Predic	dardize tor Wei	ghts	Criterion Variables		dardized ion Weigl	nts
	PV1	PV2	PV3	e de la composição de la c	CV1	CV2	CV3
der	.32	19	.91	Tenure	. 02	50	04
asian	.16	1.67	.43	Asst. Prof.	.29	10	.36
:k	.00	. 59	.29	Assoc. Prof.	.45	20	.46
anic	.02	1.10	. 54	Professor	. 54	18	. 54
ental	.03	.46	.04	Masters	16	3.53	08
	.88	07	43	Doctorate	18	3.69	.21
				Yrs. Instr.	.02	.03	31
				Yrs. Asst. Prof.	.27	.38	15
				Yrs. Assoc. Prof.	.36	.25	.02
				Yrs. Prof.	.62	00	43
				Business	.18	07	16
				Phys. Sci.	.06	.02	04
		-		Soc. Sci.	.09	.04	01
				Humanities	.10	.18	49
				PVA	.10	05	05
				HHS	.06	.02	78
			•	Education •	.18	07	58
				Canonical R	.76*	.42*	.38***

^{*}Wilks' Lambda Significant at 0.001 when converted to an approximate F. '*Wilks' Lambda Significant at 0.001 when converted to an approximate F. '*Wilks' Lambda Significant at 0.001 when converted to an approximate F.

analysis. As is the case with Table 2 the standardized weights associated with the set of predictors and set of criteria are presented. The two significant canonical R-values are .77 and .43. Both are significant at 0.001 level.

In Table 4 results of the canonical analysis for the 1984-85 study are described for N = 380 observations. The decline in the number of observations over the three-year period is a function of declining enrollment at UNC. The first two canonical R-values (.73 and .40) are statistically significant at the 0.001 level and the corresponding standardized weights for the set of predictors and criteria are reported. The standardized weights and canonical R-values for the four non-significant relationships in 1984-85 are not presented.

Standardized canonical weights are often interpreted in a manner analogous to the interpretation of standardized regression weights in multiple linear regression. It is not surprising, therefore, to see some researchers use them as indices of the relative contribution or importance of the variables with which they are associated. Because of the multicollinearity associated

nonical Solution Using Standardized Weights for Significant Relationships for N = 446

kervations (1983-84)

edictor fiables	Standardized Predictor Weights PV1 PV2	Criterion Variables	Standard Criterion CV1	
_{id} er	.30 .94	Tenure	05	.23
casian	.19 .15	Asst. Prof.	.36	.96
i. Jok	02 .32	Assoc. Prof.	.65	.98
spanic	.07 .41	Professor	.82	1.03
iental	.0905	Masters	04	21
e	.9037	Doctorate	12	05
7 7		Yrs. Instr.	.04	37
		Yrs. Asst. Prof.	.27	40
		Yrs. Assoc. Prof.	.28	.00
		Yrs. Prof.	.64	43
		Business	.18	26
		Phys. Sci.	.03	05
		Soc. Sci.	.11	07
		Humanities	.11	39
		PVA	.09	12
		HHS	.08	71
		Education	.15	50
		Canonical R	.77*	.43**

^{*}Wilks' Lambda Significant at 0.001 when converted to an approximate F. **Wilks' Lambda Significant at 0.001 when converted to an approximate F.

Canonical Solution Using Standardized Weights for Significant Relationships for N = 380 Observations (1984-85)

Predictor	Stand	ardized	Criterion	St and a	rdized
Variables	Predict	or Weights PV2	Variables	Criterio CV1	Weight:
en transcription and analysis of the second					
Gender	.25	•94	Tenure	06.	.46
Caucasian	.18	08	Asst. Prof.	.39	.55
Black	06	.15	Assoc. Prof.	.68	.30
Hispanic	. 05	.27	Professor	.73	.49
Oriental	.07	16	Masters	21	72
\ge ·	.92	28	Doctorate	30	51
	•		Yrs. Instr.	.11	50
			Yrs. Asst. Prof.	.26	42
			Yrs. Assoc. Prof.	.36	.03
			Yrs. Prof.	.80	53
			Business	.09	12
			Phys. Sci.	.03	.04
			Soc. Sci.	•08	.05
			Humanities	.04	29
			PVA	.03	.02
			HHS	02	54
			Education	.10	38
			Canonical R	.73*	.40**

^{*}Wilks' Lambda Significant at 0.001 when converted to an approximate F. **Wilks' Lambda Significant at 0.001 when converted to an approximate F.

with the set of predictors as well as the set of criteria, the standardized canonical weights suffer from the same shortcomings as those of standardized regression coefficients. Not only the signs but the magnitude of the weights can be misleading. These limitations appeared with the results presented in Tables 2, 3, and 4. For these reasons, the investigators used structure coefficients for the purpose of interpreting and explaining the results of CA. For a further discussion of this point, see Cooley & Lohnes (1976); Thorndike & Weiss (1973).

In Tables 5, 6, and 7 are presented the corresponding structure coefficients or loadings associated with the significant canonical correlations found in the three-year study at UNC. A structure coefficient or loading in CA is the correlation of a specific variable and a canonical variate. For example, in Table 5, we see that the age variable correlates .94 with the first predictor variate (PVI). In other words, the square of .94 changed to a percent indicates that 88.36% of the variance in the linear composite of the predicator variables (discrimination variables) can be explained by the age variable.

A rule of thumb is suggested by Pedhazur (1982) that structure coefficients \geq .30 be considered as meaningful or useful in explaining significant canonical correlations. In Table

Table 5
Structure Loadings for Significant Canonical Correlations for N = 492 Observations (

Predictor Variables	Structi Predict PV1	ure Load tor Var PV2	dings iables PV3	Criterion Variables		cture Loa erion Var VI CV2
Question of the						
Gender	.44	30	.81	Tenure	. 65	10
Caucasian	.20	.59	11	Asst. Prof.	52	.08
Black	03	.03	.08	Assoc. Prof.	12	. 04
Hispanic	12	. 05	.28	Professor	. 71	07
Oriental	03	30	08	Masters	31	.10
Age	.94	. 01	28	Doctorate	.33	.11
				Yrs. Instr.	08	08
				Yrs. Asst. Prof.	.28	.23
				Yrs. Assoc. Prof.	.69	.09
				Yrs. Prof.	.78	07
				Business	11	09
		•		Phys. Sci.	.16	.05
				Soc. Sci.	00	.07
				Humanities	00	.07
				PVA	00	11
			•	HHS	21	.08
				Education	.07	05

vacture Loadings for Significant Canonical Correlations for N = 446 Observations (1983-84)

dictor lables	Structur Predicto PV1	re Loadings or Variables PV2	Criterion Variables	Structure Lo Criterion V CV1	
de r	.41	.84	Tenure	.53	.00
asian	.17	18	Asst. Prof.	43	
35 an					00
anic	05	.10	Assoc. Prof.	09	. 05
inic	12	.26	Professor	.57	.02
ntal	00	06	Masters	26	15
	.93	25	Doctorate	.27	.15
			Yrs. Instr.	05	19
			Yrs. Asst. Prof.	.22	11
			Yrs. Assoc. Prof.	.46	.04
	•		Yrs. Prof.	.61	00
			Business	13	.00
		·	Phys. Sci.	.11	. 09
			Soc. Sci.	.04	.13
4.			Humanities	01	06
\$			PVA	01	.08
			HHS	10	25
¥			Education .	.05	05

Table 7

Structure Loadings for Significant Canonical Correlations for N = 380 Observations (19)

Constitution of the second

Predictor Variables	Structure Predictor PV1	Loadings Variables PV2	Criterion Variables	Structure Loadi Criterion Varia CVI
Gender	.35	.87	Tenure	. 64
Caucasian	.20	24	Asst. Prof.	 59 .
Black	06	.06	Assoc. Prof.	~.14 .
Hispanic 🕒	14	.29	Professor	.69
Oriental	02	07	Masters	 19 -
Age	.94	19	Doctorate	.19
			Yrs. Instr.	 06 -
			Yrs. Asst. Prof.	.13 -
			Yrs. Assoc. Prof.	.41
			Yrs. Prof.	.59
			Business	14
			Phys. Sci.	.14
			Soc. Sci.	.04
		t	Humanities	01 -
			PVA	05
			ннѕ	14 -
			Education	.05 -

1e 8

ful Structure Coefficients (Loadings) in Explaining Relationships between Significantly related Canonical Variates

Discrimination Variables	1982-8 PV1	3 (N = PV2	492) PV3	1983-84 PV1	(N = 446) PV2	1984 (N = 380) PV1 PV2
_{der} wasian wak	*+	*- *+	*+		*+	*+ *+
_{sp} anic						
ental		*_				
i A	*+			*+		*+
University Status Variables	1982-8: CV1	3 (N = CV2	492) CV3	1983 <i>-</i> 84 CV1	(N = 446) CV2	1984 (N = 380) CV1 CV2
े ure	*+			*+		*+
. Prof.	*_			*=		*-
c. Prof.						
fessor	*+			*+		*+
ters	*-		*-			
torate . Instr. . Asst. Prof.	*+		*+			
Assoc. Prof.	*+			*+		*+
Prof. iness Sci	*+			*+		*+
. [™] Sci. anities			*+			
			*-			
cation onical R	.76	.42	.38	.77	.43	.73 .40

Structure coefficients \geq .30 were considered as meaningful (Pehhazur's criterion). A "*+" represents a positive coefficient \geq .30 and a "*-" refers to a negative structure loading \geq .30.

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8 the structure coefficients which are \geq .30 are starred as positive or negative depending on the sign of the structure coefficient. The purpose of this table is to present the results for the three consecutive years at UNC in such a way that the significant canonical R-values might be interpreted in terms of the set of predictors and the set of criteria.

In reviewing the starred variables in Table 8 it can be seen that the linear combination of predictor variables in the first canonical R for each of the three years has a positive structure loading on gender and age. Thus, PVI might be conceptualized as a factor representing older males. If we focus on the corresponding set of university status variables (CVI) for the three years we see positive loadings on tenure, professor, years associate professor, years full professor and a negative loading on assistant professor. For 1982-83 only we see a negative loading on masters and a positive loading on doctorate. The loadings on the criterion variate for all three years suggest that CV1 reflects the factor of an experienced professional -- one with tenure, higher academic rank, and more experience at the associate or full professor level. It is interesting to note that degree status (criterion set) seems unrelated to age and gender (predictor set) in the last two years of study. As one

investigates the pattern that relates the predictor variate with the criterion variate in the second canonical R and in the case of 1982-83 the third canonical R, the picture becomes less clear. In 1982-83, the positive and negative loadings in PV2 suggest a factor of female Caucasian in the predictor variate whereas no significant loading was detected in the criterion variable set (CVI). From a discrimination claims point of view this might be interpreted as a positive finding. The discrimination factor in PV2 (female Caucasian) seems related to university status factor variables in no systematic way. Similarly, the PV2 seems to be a gender factor for both 1983-84 and 1984-85 but is unrelated to any university status variable in CV2 for both years. In 1982-83 a third significant canonical R was found. PV3 in this year seems to reflect a gender factor and this factor seems to show that males tended to have the doctorate, were not instructors, were social science faculty and not HHS faculty members. This gender university status pattern for 1982-83 did not show up in subsequent analyses for both 1983-84 and 1984-85 and should be considered another positive finding from a discrimination claims point of view. Finally, it should be observed that race as a discrimination variable did not exhibit a high loading in each of the three years. Race seems unrelated to the linear composite of university-status variables.

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In Table 9 are presented the percent of the variance in the linear composite of the university-status variables (criterion

Table 9

Percent of Variance in Set of University Status Variables Linear Composite Explained by

Discrimination Variables

1

Discrimination Variables	1982- CV1	-83 (N = CV2	492) CV3	1983-84 CV1	(N = 446) CV2	1 984-1 CV1	989
Gender	11.36	13.10	22.83	10.41	23.55	6.74	19
Caucasian	2.39	8.95	9.13	1.79	2.45	2.22	3
Black	0.06	0.08	0.18	0.19	0.38	0.25	
Hispanic	0.95	1.01	2.17	0.97	2.25	1.17	2
Oriental	0.09	1.78	1.88	0.00	0.08	0.04	C
Age	51.74	51.75	52.94	52.45	53.65	48.66	49
Canonical R	.76	.42	.38	.77	.43	.73	

¹Only criterion variable linear composites are presented which are associated with canonical R-values which are significant beyond the 0.001 level.

variate) that can be explained by each of the six discrimination (predictor) variables for the significant canonical R-values found. Results in this table seem to confirm that age was the dominant variable over the three years—it explained about 50% of the variance in each of the criterion variates. Gender appeared to be a much less significant factor as the percent of variance for each criterion variate explained ranged from about 7% to a high of 24%. Race as a factor was not significant as the percent of variance of the criterion variate it was able to explain ranged from a low of 0% to a high of 9%.

In summary, the results of CA seem positive from the issue of discrimination claims in higher education. While the older-male relationship with the professional-experience factor was detected in the three-year analysis, the relationship has historical roots and is less pronounced today. No other gender or race factors were found to be linked in any systematic way to any university-status factors.

Discriminant Analysis

To investigate further the possibility of discrimination patterns in tenure and promotion decisions, a statistical technique known as discriminant analysis (DA) was applied to data for the academic years 1982-83, 1983-84 and 1984-85. The DA

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method analyzes one variable such as tenure status by comparing it with a group of variables called independent variables or predictors. Since the tenure status variable is a binary variable, DA determines a set of weights which maximizes the criterion for group membership, called the discriminant function. This function serves as the basis for attempts to "classify" each faculty member into one of the two original groupings, tenured or nontenured. Two linear combinations of the independent variables are formed to "characterize" group membership.

After the linear combinations are determined, the values of the predictors for each individual are used to calculate discriminant scores which will indicate which of the two groups the individual's profile most closely resemble. This measure is given by posterior probabilities of group membership. After the analysis is completed for all individuals, those observations which are misclassified can be analyzed for inequities or other irregularities.

For the three academic years of interest, DA was conducted using the five variables tenure status, professor rank, associate professor, assistant professor, and instructor as the criterion variables individually. The predictors were age, gender, race, highest degree, years in rank, and discipline. Tables 10 through 12 present the linear discriminant function for each criterion variable and the resulting classifications and misclassifications for the three years.

Table 10

Discriminant Function (1982-83)

Age	Education	SHH	PVA	Humanities	Soc.Sci.	Phys. Sc1.	Business	Yrs. Prof	Yrs. Assoc.	Yrs.Asst.	Master		frs.Instr.	Oriental	Hispanic	Black	Caucastan	Gender	00000	Doctorate	Constant	Predictors	
	445.71	453.42	449.49	454.85	445.90	445.88	451.57	54	-1.54			776.30	31	147.91	152.39	149.88	153.16	9.0		227.82	-428.52	•	Tenure
~	_	453.78			447.34																-436.40	."	
÷	446.83	454.68	450.82	455.68	446.73	447.28	452.55	12	1.33		-	225.68	24	149.91	153.20	149.40	133.37	153 87	5.96	228.46	-431.07	•	Professor
.90	3 449.26	_		457.61			454.96														-443.23	-	Ŕ
	445.44	452.82	449.50	454.50	445.	*****	451.15			-1.0	<u>.</u> .	226.21	21.18	149.44	153.44		Š	153.99	5.81	228.24	-430.27	•	<u>Associate</u>
83 .85			_	\$0 453.14																230.51		-	ite
i	443.69	***		AS -10	K 13A	45.72	446 89	451.5	٠.	5	. . .	223.55	-	100.00		157 %	153.29	159.22	5.32	227.24	-436.00		Assistant
				449_69	454.85	16.11	145.98	7 451.52	51	6 -1.45	10	225.88	23		Ē :	152.74	150.02	153.37	5.76	227. 64	-428.38	-	. 10
	e	446.39	453.33	452.01	456.66	446.25	445.23	451.61	68	-1.42	. 37	235.62		3	145.66 66	152.27	150.04	150.98	8. 4	240.55	439.13	•	Instructor
·	-	•	_		-		446.32						331 40			152.93	149.99	154.44	4.52	221.68	-418.89		_ FR

Table 12

Discriminant function (1984-85)

Criterion Variable

Innure Professor Associate Associate Assistant List 0 1 0 0 1 0 0 1 0 0 1 0 0 1 0 0 0 1 0 0 0 0	. 74	.93	.9	.93	.	. 89	. 88	. 88	.88	. 88	Age
Tenure Professor Associate Associate Associate Assistant Libition 0 1 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 0 1 0 0 1 0 0 1 0 0 1 0 0 0 0 0	92	95.07		93.32	91.69	94.05	98.86	95.63	95.16	94.34	Education
	102	101.67		% . %	97.37	101.11	106.58	103.06	102.10	101.81	XXX
Industry Professor Associate Associate Assistant Assistant Assistant 0 1 0 0 1 0 1 0 0 1 0 0 1 0 0 1 0	8	101.98		190.69	98.91	100.42	105.22	101.87	102.36	100.22	PVA
Indust Professor Associate Assistant A	107.	112.52		189.61	188.86	111.05	115.24	112.44	1111.47	111.50	Humanities
Tenure Professor Associate Associate Assistant A	92.	94.47		92.92	91.69	93.71	97.53	94.98	95.04	93.83	Soc.Sci.
Industrial Professor Associate Assistant <	92.	94.22		93.66	90.57	93.26	99.78	95.32	94.54	93.58	Phys. Sci.
Ienure Professor Associate Assistant A	9	93.99		93.26	91.27	93.66	98.14	95.16	93.57	94.33	Business
Tenure Professor Associate Assistant A		82		50	-1.39	88	.55	:	- 1	87	Yrs. Prof
Tenure Professor Associate Assistant A	<u>-</u>	-1.43		27	89	-1.36	-1.18	-1.39	88	-1.64	Yrs. Assoc.
Tenure Professor Associate Assistant A		.65		:	.41		.45	•	.98	-	Yrs.Asst.
Tenure Professor Associate Assistant A	100.	491.48		494.57	403.40	401.55	401.13	401.16	395.57	402.94	Master
Tenure Professor ASSOCIATE ASSISTANT LINSTITUCENT 0 1 0 1 0 1 0 -366.12 -372.00 -368.21 -379.68 -367.77 -373.13 -379.33 -366.58 -369.82 404.68 399.18 404.08 406.22 403.92 406.66 410.25 495.92 404.73 10.21 11.38 10.74 11.49 10.46 10.34 10.69 10.53 10.99 195.52 200.25 197.14 198.60 197.17 199.71 204.31 198.50 195.97 190.90 196.38 193.25 196.32 192.43 193.51 198.55 193.74 191.95 195.23 201.73 197.11 198.10 197.32 199.96 203.63 198.43 196.54 186.68 194.59 189.58 192.57 189.41 193.49 201.28 191.63 187.92	<i>!</i> .	-1.05		39	68	85	91	- 89	28	-1.07	Yrs.Instr.
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Tenure Professor Associate Assistant A	197.	196.54		203.63	199.96	197.32	198.10	197.11	201.73	195.23	Hispanic
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Tenure Professor Associate Assistant Assistant Assistant 0 1 0 1 0 1 0 -366.12 -372.00 -368.21 -379.68 -367.77 -373.13 -379.33 -366.58 -369.82 -404.68 404.68 399.18 404.08 406.22 403.92 406.66 410.25 405.02 404.73 10.21 11.38 10.74 11.49 10.46 10.34 10.69 10.53 10.99	198.	195.97		204.31	199.71	197.17	198.60	197.14	200.25	195.52	Caucasian
Tenure Professor Associate Assistant Assistant Assistant 0 1 0 1 0 1 0 -366.12 -372.00 -368.21 -379.68 -367.77 -373.13 -379.33 -366.58 -369.82 404.68 399.18 404.08 406.22 403.92 406.66 418.25 405.02 404.73	50	10.99		10.69	10.34	10.46	11.49	10.74	11.38	10.21	Gender
Tenure	398.6	404.73		410.25	406.66	403.92	406.22	404.08	399.18	404.68	Doctorate
Tenure Professor Associate Assistant O 1 0 1 0 1 0 1	-360.	-369.82		-379.33	-373.13	-367.77	-379.68	-368.21	-372.00	-366.12	Constant
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	n	Instructor	17	Assistant	m	Associate	R	Profess		Tenure	

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Table 1	3	***		CH	1000 在100000000000000000000000000000000						**************************************			
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FROM	0 1	0 269 22 291	T0 1 8 193 201	T 277 215 492	87	0 0 1 T	T0 1 252 19 271	1 174 175	T 253 193 446		0 1 T	0 208 19 227	0 1 0 153 153	2 1 3
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 ^{0 -} indicates individual does not belong to class
 1 - indicates individual does belong to class

FROM - is ACTUAL STATUS TO - is PREDICTED STATUS

Table 14 R^2 Values for Full and Restricted Models for 1982-83 through 1984-85

Model	Academic Year					
	1982-83	1983-84	1984 -85			
Full Model (FM)	.8630 A	.8691 A	.9006 A			
FM - Discrimination Set	.8510 B	.8616 B	.8990 A			
FM - Gender	.8580 B	.8651 B	.8995 A			
FM - Race	.8626 A	.8680 A	.9002 A			
FM - Age	.8480 B	.8659 B	.9005 A			

Note: \mathbb{R}^2 values in a column with the same letter as the full model are not significantly different from each other. All P's<01.

\$77.73

As seen in the above tables, the number of misclassifications in all five analyses decrease from 1982-83 to 1984-85. Several policy changes within the institution provide possible explanations for this pattern. These relationships will be discussed in the section entitled Contextual Analysis.

Upon examination of the individual cases identified by DA as misclassified, the majority were explained by rational, nondiscriminatory factors or by historical factors due to evolving standards at UNC. For example, in the year 1984-85, UNC has 72 faculty members who are not tenured. The DA method indicates two of these individuals possess values for the predictors which more closely resemble the individuals who are tenured.

The first faculty member is a male who has a special seven year agreement with the Board of Trustees in lieu of tenure. The second faculty member is a male who is hired annually on state grant money through the Colorado State Vocational Education Program. Even though he has excellent credentials, he is on soft money and is therefore not tenured.

The majority of the 26 faculty members who are tenured but more closely resemble the nontenured group are faculty members who do not possess the doctorate. These faculty members were tenured in the period from 1965-1975 when the availability of qualified

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faculty and the standards for obtaining tenure were quite different from the period since 1975.

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Similar analyses were performed for the misclassifications for each rank. Few individual cases were identified which required further attention. In no instance was there any pattern of cases which would indicate systemic discrimination by the University on the basis of gender, age or race.

For 1984-85, the ranks of associate professor and assistant professor had a number of misclassifications from 0 to 1 (See Table 13). Upon further study, most of the misclassifications of this nature were situations in which a faculty member possessed a higher rank than the DA method predicted for the individual. The DA method consistently misclassified such individuals in all ranks for each year. These individuals had been promoted prior to 1976 when standards for promotion began to change at the institution.

This technique is an excellent tool for identifying general patterns as well as individual faculty members who may have been treated differentially. Certainly this method cannot be treated in isolation; however, it provides additional information to the institution in an attempt to correct whatever inequities which may exist. Both the canonical correlation and discriminant analyses show the variables of tenure status and rank are not "tainted" with respect to the discrimintation variables. Therefore, the variables of tenure status and rank may be used in the multiple regression analysis of salaries to improve the overall predictive efficiency.

Multiple Regression Analysis

Multiple regression (MR) analyses were performed to examine the relationship between salaries of full-time faculty and a set of discrimination variables, i.e., gender, race and age, for the years 1982-83 through 1984-85. Predictor vectors were coded for the MR analyses to reflect an individual's gender, race, age, qualifications, academic discipline, rank, tenure status, years spent in each rank and years before receiving tenure.

Justification for including variables related to a faculty member's status within the institution was provided by the results of the canonical correlation analysis. Recall that there was no relationship between the academic status variables and the discrimination variables of gender and race. That is to say, no evidence was found that rank, tenure status, time in rank and time before receiving tenure were the result of discriminatory practices.

For each of the three years under consideration, salaries were regressed on the variables listed in Table 1 (the full model). Subsequently, salaries were regressed on a model containing all of the variables in the full model except for the set of discrimination variables: gender, race and age (the restricted model). Differences in R² values for the full and restricted models were tested by means of the F-distribution (Pedhazur, 1982). If the set of discrimination variables was found to account for a significant proportion of variance in

salaries, the variables were examined one at a time to identify the specific source(s) of discrimination. Diagnostics were also performed to determine if the collinearity assumption had been violated. R^2 values of the full and restricted models for each of the three years are presented in Table 14.

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Results of the MR analyses for the 1982-83 year show that the full model accounted for 86% of the variance in faculty salaries, F(22,469)=133.93, p<01, while the restricted model accounted for 85% of the variability in salaries, F(17,474)=159.42, p<01. Although the difference in R^2 values for the two models was small, it was statistically significant, F(5,469)=8.21, p<01. Further analyses of the 1982-83 data found that gender, F(1,469)=17.11, p<01 and age, F(1,469)=51.35, p<01, accounted for a significant proportion of the variance in faculty salaries. There was a tendency for males to earn higher salaries than females and the relationship between age and salary was found to be positive. No evidence of discrimination on the basis of race was detected by the analysis, F(3,469)<1.

A pattern similar to that found in 1982-83 emerged from the 1983-84 salary data. The squared multiple correlation coefficient for the full model was .87, F(22,423) = 127.61, p < 01, while the R^2 value of the restricted model was .86, F(17,428) = 156.79, p < 01. Again deleting the set of discrimination variables from the full model produced a statistically significant decrease in R^2 , F(5,423) = 4.83, p < 01. Subsequent analyses show once again that

gender and age accounted for a significant proportion of the variance in salaries, F(1,423) = 12.90, p < 01; F(1,423) = 10.32, p < .01, respectively. The increment in the proportion of variance in salaries attributable to race was not significant, F(3,423) = 1.18.

Implementation of the new University salary model for 1984-85 virtually eliminated discrimination in salaries on the basis of gender, race or age. For the full model R^2 = .90 while the restricted model resulted in an R^2 = .89. The difference in R^2 values for the full and restricted models was not statistically significant, F(5,357) = 1.14, p<.05.

In summary, evidence was found that males earned higher salaries than females from 1982-83 to 1983-84; however, the difference between male and female salaries was eliminated after the implementation of a new salary model. There was also a tendency for older faculty members to earn higher salaries than younger faculty members during the same period. Similarly, the relationship between age and salary was eliminated in 1984-85. There was no evidence of salary discrimination on the basis of race during any of the three years under consideration.

Contextual Analysis

Before discussing the results, a brief history of UNC is required in order to understand the context within which the results occurred. UNC is a former normal school which was founded in 1889. The institution evolved from the normal school to a teacher's college (1935), to a state college (1957), to a

university (1970) as have many other similar institutions in the country. However, UNC differed in one significant aspect. During the 1920-1940 period, UNC embarked on a unique path of offering many graduate programs particularly at the doctoral level.

Instead of developing the programs from a solid base of bachelor degree programs to a broadly based masters degree program to the doctoral level, UNC jumped immediately to the doctoral level.

This lack of breadth eventually caused serious problems of enrollment and quality of doctoral work in the late 1970's.

To further compound problems, the institution engaged in the practice of hiring its own graduates, particularly in the late 1950's and 1960's. These faculty members were tenured and promoted rapidly under standards which were less rigorous than those that exist now at UNC. Tenure was nearly automatic after three years of service and promotions were granted every four years. Thus a faculty member would normally become a tenured full professor after eight years of service. Many did not possess the credentials which would justify a similar rank or status at another institution of higher education. Thus the faculty member was "trapped" at UNC unless the faculty member was willing to take a lower rank at a different institution. All these factors resulted in an older faculty that was not mobile in the market place.

In addition, enrollment began to decline in 1977 and with one exception continued to decline in the 1980's. The institution's

enrollment has fallen from a peak of 11,770 in 1977-78 to 8,800 in 1984-85.

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All these factors have led to numerous policy changes which are important to place the analysis in context. Prior to 1982-83, tenure and promotion decisions were made by a process which called for departmental recommendations to be passed to the council of deans who made a strong recommendation rarely overturned by the vice president or president. Little was known of the criteria or method of decision used by deans. Beginning in 1982-83, the council of deans was replaced by a committee of faculty members and the criteria for tenure and promotion were more stringent and clearly defined. This change was the final step in a movement towards higher tenure and promotion standards initiated in the late 1970's.

As a result, obtaining tenure and/or promotion is considerably more difficult now than at any time before. In fact there are numerous instances in which faculty members possess a rank for which they would no longer be qualified under the new policies. These tougher standards which have been used for faculty members hired since 1976 cause numerous misclassifications in the DA analysis presented in the previous section.

With the enrollment decline came the need to reduce staff, faculty and the budget. In 1982, the decline culminated in a major reduction in force which led to the termination of 47 faculty members, 38 of whom were tenured. From 1977-78 to

1984-85, the University lost 155 faculty positions or 24% of the faculty positions it employed in 1977-78. The faculty in 1984-85 is considerably younger than its counterpart which existed in 1982-83.

In 1983-84, the institution initiated an early retirement plan to encourage faculty members to retire. Forty-two (42) faculty members accepted the offer and retired at the conclusion of the 1983-84 academic year.

These two events, the reduction in force and the early retirement plan, help explain the dramatic improvement in the results of both the regression analysis and the discriminant analysis classification analysis over the three-year period. UNC lost approximately 90 of its older faculty members during this period and was able to hire a significant number of new faculty members. Thus a substantial change in the demographics of the remaining faculty has occurred. The improving pattern of rank and tenure classifications is to be expected as fewer faculty members who were tenured or promoted under past policies are employed at UNC.

Finally, in an effort to improve the salaries of its faculty and to correct individual inequities, UNC developed a new faculty salary model which was implemented for the 1984-85 year. This new model called for a survey of 29 peer institutions to be selected on the basis of similar role, mission, programs, enrollment and budget to that of UNC. At the same time the institution developed

a comprehensive evaluation system which was used to help determine salaries. Therefore, a faculty member's salary was determined by the rank, discipline, time in rank and the evaluation rating for the previous year.

This new salary model led to a substantial redistribution of salary dollars among the faculty. No salary was reduced; however, a number of faculty members had their salary frozen. In contrast, a number of faculty members received salary raises of between \$6,000-\$9,000 or an increase of 20% to 30%.

Any faculty member who received an unsatisfactory evaluation received no salary raise. There were approximately 20% of the faculty who fell into this category for 1984-85 salary determinations. Thus the salary patterns which had existed in 1982-83 and 1983-84 changed dramatically for 1984-85. The purpose for the change was two-fold as mentioned above: (a) to improve salaries of the faculty at UNC relative to peer institutions and (b) to base salary decisions on rational factors such as qualifications and evaluations rather than historical factors or inconsistent policies of the past.

The results of the regression analysis clearly demonstrate the success of the new salary model in neutralizing the gender factor in salaries. The effects of the reduction in force effective in 1983 and the early retirement plans effective in 1984 are clearly seen in the analysis of the age factor over the three years. These factors combined with the new salary model have

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produced a salary structure which has no indication of age dependency.

The race factor was not significant in any of the three years analyzed in this study. UNC has undergone significant changes both externally imposed and internally imposed. The statistical techniques used to assess the status of salaries and tenure and promotion decisions confirm the changes have improved the consistency of these decisions. When analyzed within the context of evolving institutional policies, these statistical tools can provide valuable insight into the status of decisions made with regard to salaries, tenure or promotion.

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Multiple Comparisons Via Multiple Linear Regression: Learning the Obvious Takes Time

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John D. Williams

The University of North Dakota

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Perhaps a best starting point is at the beginning—the beginning of my involvement in multiple linear regression ala Ward, Bottenberg and Jennings. A presession to the AERA annual meeting in New York in 1967 was my first exposure to this type of analysis. I must admit something less than being fully enthralled with their ideas at the time. Despite computer accessibility for the five day workshop, I didn't actually run any programs. To me it was just a new fad. When getting back to Grand Forks (N.D.) I did feel some pangs of conscience and tried running a simple ANOVA by regression. The problem was a three group situation; I was trying to run:

$$y = b_1 x_1 + b_2 x_2 + b_3 x_3 + e_1$$

[1]

where

 $X_1 = 1$ if a member of group 1, 0 otherwise,

 $X_2 = 1$ if a member of group 2, 0 otherwise,

 $X_3 = 1$ if a member of group 3, 0 otherwise,

 $\mathbf{b}_1,\;\mathbf{b}_2,\;\mathbf{b}_3$ are regression coefficients,

Y = the criterion score, and

 e_1 = the error in prediction with this model.

The program used at the presession was DATRAN, a forerunner of LINEAR (which of course, I didn't actually use). The program available to me back

in North Dakota was a stock IBM program; in retrospect, such stock programs typically have automatic inclusion of a unit vector (or constant). Well, what happened next is both a descriptor of something about my personality (stubborn) or possibly lack of intelligence (slow). On a daily basis for seven weeks, (that's 35 times) I unsuccessfully tried running the program exactly as shown in equation 1 without any change. I thought possibly there was something wrong with the computer or the program; never did it cross my mind that I might have made a conceptual error. Finally, I started monkeying with the input (I was convinced the stuff in Bottenberg and Ward, 1963, was wrong). Well, I finally made the right mistake, and the program actually worked correctly. One form of that mistake is as follows:

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 $Y = b_0 + b_1 X_1 + b_2 X_2 + e_1$. [2] The difference between equation 2 and equation 1 ostensibly is the exclusion of b_0 in equation 1 and the exclusion of $b_3 X_3$ in equation 2.

Also, I now know that equations 1 and 2 are reparameterizations of one another. There are also some other "obvious" things about equation 2; it took me only four years to discover some of the obvious.

Equation 2 can allow not only a simple ANOVA, but also describes some important aspects of Dunnett's (1955) test (Williams, 1971); \mathbf{b}_0 is not just a constant, but is equal to \mathbb{Y}_3 , the so-called left out group. Also, $\mathbf{b}_1 = \mathbb{Y}_1 - \mathbb{Y}_3$ and $\mathbf{b}_2 = \mathbb{Y}_2 - \mathbb{Y}_3$. Equation 2 could be rewritten as:

In addition to an ANOVA, other simple designs can be shown in a regression lay-out, such as the analysis of covariance, the t test, and treatments x subjects designs. The use of equations such as equation 2

to complete these designs was shown in Williams (1970). As usual, I had no idea at the time of the relationship to multiple comparisons. In some ways, the relationships are so simple and direct that it gives me cause for some degree of humility to remember how long it took me to discern the obvious again.

Through the use of full and restricted models, a process to test comparisons equivalent to Tukey's (1953) test was shown (Williams, 1974a). With three groups, beginning with equation 1, $Y = b_1 X_1 + b_2 X_2 + b_3 X_1 + b_4 X_2 + b_5 X_3 + b_5 X_4 + b_6 X_5 + b_6 X_$ $b_3X_3 + e_1$. Now suppose the test of $\overline{Y}_2 = \overline{Y}_3$ is of interest. In terms of the regression coefficients $b_2 = b_3$ is the appropriate restriction.

Then
$$Y = b_1 X_1 + b_2 X_2 + b_2 X_3 + e_2$$
 or

$$Y = b_1 X_2 + b_2 (X_2 + X_3) + e_2.$$

Let
$$V_1 = X_2 + X_3$$
; then

$$Y = b_1 X_1 + b_2 V_1 + e_2.$$
 [4]

Equation 4 can be reparameterized so that the unit vector (constant term) is reintroduced by excluding either X_1 or V_1 . Excluding X_1 yields:

$$y = b_0 + b_2 V_2 + e_2.$$
 [5]

Testing t =
$$\sqrt{F}$$
 = $\sqrt{\frac{(R_2^2 - R_5^2)/1}{(1 - R_2^2)/(N - K)}}$ yields a t appropriate to

testing V_2 to V_3 .

On the other hand, there is an easy way to run Tukey's test by regression. All that is necessary is the set of reparameterizations of equation 1:

$$y = b_0 + b_1 x_1 + b_2 x_2 + e_1,$$

$$Y = b_0 + b_1 X_1 + b_3 X_3 + e_1,$$
 [6]

and
$$Y = b_0 + b_2 X_2 + b_3 X_3 + e_1$$
. [7]

Here, the test of the computed t values is identical to a similar test for Tukey's test. (It took a full three years after doing the same thing with Dunnett's test to realize that Tukey's test could be accomplished through successive psuedo-Dunnett's tests). One complication is that most published studentized range tables are in terms of q, rather than in terms of testing the regression coefficients for significance. A table showing a direct solution using tests on the (partial) regression weights is given in Williams (1976, 1980).

In that I routinely would find all simple reparameterizations of an equation for an ANOVA solution, taking seven years to discover the obvious says something.

Two-Way Disproportionate ANOVAs

The two-way analysis of variance with disproportionate cell frequencies has been discussed in many different publications; Bottenberg and Ward (1963) showed a regression solution for the general case, and Jennings (1967) concentrated on the disproportionate situation. To be honest, I had a lot of trouble understanding the Jennings article, so I tried to go about doing what I could understand from the original Bottenberg and Ward presentation. One aspect of Bottenberg, Ward and Jennings in their various writings is a concern for explicitly stating exactly the hypothesis being tested through the use of a restriction on the regression coefficients. This aspect has been both a blessing and a curse; it is a blessing in the sense that the approach allows a precise methodology. It is a curse in that users are often at a disadvantage because of the cognitive completixity and relative mathematical sophistication required in comparison to traditional

analysis of variance methodologies. It could be arqued that a middle ground can be attempted; to some degree, that middle ground was something I tried to do (Williams, 1974b).

As an example of a two-way ANOVA with disproportionate cell frequencies the following data set was originally published in Williams (1972):

Data for Disproportionate Two-Way Analysis of Variance

Effect	2.15 N	Effect		
	B ₁		B ₂	B ₃
A ₁ .	8 6 4			6 2
A ₂	10		7 5 4 4 3	10 9 7 5 4

The solution given (1972) that was meant to simplify the process was to form four models:

$$y = b_0 + b_1 x_1 + b_2 x_2 + b_3 x_3 + b_4 x_4 + b_5 x_5 + e_3;$$
 [8] where

 $x_1 = 1$ if from an individual in cell 1 (row 1, column 1), 0 otherwise;

 $x_2 = 1$ if from an individual in cell 2 (row 1, column 2), 0 otherwise;

 $x_3 = 1$ if from an individual in cell 3 (row 1, column 3), 0 otherwise;

 $X_4 = 1$ if from an individual in cell 4 (row 2, column 1), 0 otherwise;

 χ_5 = 1 if from an individual in cell 5 (row 2, column 2), 0 otherwise; and b_0 to b_5 are regression coefficients for this model.

$$Y = b_6 + b_7 X_7 + e_4;$$
 [9]

where

 $x_7 = 1$ from an individual in row 1, 0 otherwise and b_6 , b_7 are regression coefficients for this model.

 $Y = b_8 + b_9 X_9 + b_{10} X_{10} + e_5;$ where

 x_9 = 1 if from an individual in column 1, 0 otherwise; x_{10} = 1 if from an individual in column 2, 0 otherwise; and b_8 , b_9 and b_{10} are regression coefficients for this model.

 $Y = b_{11} + b_{12}X_7 + b_{13}X_9 + b_{14}X_{10} + e_6.$ [11]

Now a solution in terms of sums of squares can be given as follows:

From: equation 8, SS_{ATTRIBUTABLE} = 80.80;

SS_{DEVIATION} = 51.20;

equation 9, SS_{ATTRIBUTABLE} = 20.36;

equation 10, SSATTRIBUTABLE = 37.43 and

equation 11, SSATTRIBUTABLE = 80.25.

This information could be used to construct a fitting contants solution or a hierarchical solution (Cohen, 1968) or the solution described by Jennings (1967); although Jennings laboriously goes through the process of testing hypotheses through restrictions on a reparameterization of the full model:

Y = $b_1X_1 + b_2X_2 + b_3X_3 + b_4X_4 + b_5X_5 + b_6X_6 + e_3$. [12] This model corresponds to equation 8, except that the unit vector is omitted (b_0) and the sixth cell is represented through b_6X_6 . Because my solution, while it coincides with Jennings, can be addressed without adjusting the sums of squares as must be done for a fitting constants solution or a hierarchical solution, I called this solution the "unadjusted main effects" solution—in retrospect, a poor choice of names. It was called this because of the means of extracting the sums of squares—but its usefulness is because it corresponds to the Jennings solution. That

by the way, is another story—I spent an hour and a half convincing Earl that my solution gave the same results as his; at first he was skeptical. Finally, he accepted that, "computationally, their respective sums of squares was the same," but thought only people such as myself who understand both approaches and used my approach as a computational short cut should use it; if you didn't know what hypotheses were being tested, you probably shouldn't use it. I thought Earl was being a little harsh back in 1972, but today I'm coming closer to agreement with that position.

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In particular, it could be noted that the so-called "full rank model" as described by Timm and Carlson (1975), and which in fact they describe using my (1972) data set, has no better claim to being a full rank model solution than Jennings (1967); the hypotheses tested by these and other approaches are considered in Williams (1977a). It is unfortunate that the Timm and Carlson (1975) solution might be seen by some as "standard practice" or "state of the art". The issue really is, which hypotheses are of greatest interest? If the Timm and Carlson hypotheses are truly of the greatest interest, they can be addressed via the Bottenberg and Ward approach.

A summary table that computationally tests hypotheses proportional to cell frequencies such as proposed by Jennings can easily be formed from the information from equations 8, 9, 10 and 11:

 $SS_{ROWS} = 20.36$; $SS_{COLS} = 37.43$;

ss_{RC} = 80.80 - 80.25 = .55;

SS_{within} = 51.20. The summary table is as follows:

Source of Variation	df SS	MS	F
Rows	1 20.36	20.36	4.77
Columns	2 37.43	18.72	4.38
RXC	2 .55	.28	.07
Within	12 51.20	4.27	

In regard to multiple comparisons in a two-way layout, equation 12 is an appropriate starting point. The number and type of comparisons (contrasts) would be important for deciding on the type of test (Dunnett's, Tukey's, Scheffe's, 1959, and Dunn's, 1961). As an example of constructing a contrast to test a hypothesis of interest, suppose the researcher wants to compare column 1 to column 2, weighing the cells by their size, the hypothesis, in terms of sample means, is:

$$\frac{3\overline{Y}_1 + 1\overline{Y}_4}{4} = \frac{2\overline{Y}_2 + 5\overline{Y}_5}{7} .$$

In terms of the regression coefficients.

$$\frac{3b_1 + b_4}{4} = \frac{2b_2 + 5b_2}{7}$$

Unraveling and solving for b_1 yields: $b_1 = 8/21b_2 + 20/21b_5 - 7/21b_4$. Substituting this restriction into equation 12 yields:

$$Y = (8/21b_2 + 20/21b_5 - 7/21b_4)X_1 + b_2X_2 + b_3X_3 + b_4X_4 + b_5X_5 + b_6X_6 + e_7;$$
[13]

or

$$Y = b_2(X_2 + 8/21X_1) + b_3X_3 + b_4(X_4 - 7/21X_1) + b_5(X_5 + 20/21X_1) + b_6X_6 + e_7.$$
 [14]

Reparameterization with $b_6 = 0$ yields:

$$Y = b_0 + b_2(X_2 + 8/21X_1) + b_3X_3 + b_4(X_4 - 7/21X_1) + b_5(X_5 + 20/21X_1) + e_7.$$
 [15]

Equation 14 can be used in programs where unit vectors can be ommitted. Its reparameterization, equation 15, is useful when a unit vector is automatically incorporated into a regression solution. Equations 8 and 12 (full models) yield R_F^2 = .61212. Equations 14 and 15 (restricted models) yield R_F^2 = .38544. Then:

$$t = \sqrt{F} = \sqrt{\frac{(R_F^2 - R_R^2)/1}{(1 - R_F^2)/12}} = 2.648.$$

This t value should be tested against an appropriate table depending upon the type and number of total comparisons considered by the researcher.

This approach to multiple comparisons is probably much closer to the approach of Jennings and Bottenberg and Ward than I would have considered 10 to 15 years ago. Additional considerations regarding multiple comparisons in the two-way analysis of variance ban be found in Williams (1980).

Multiple Comparisons in the Analysis of Covariance

Students would often ask questions such as, "How do you do multiple comparisons on adjusted means in the analysis of covariance?" I've often been impressed with questions students ask; I'm sure they've been less impressed with at least some of my answers. Well, for several years, I didn't have any good answer to the aforementioned question (other than, "That's a good question.") and as the answer finally came to me, there was far more embarrassment than awe. The "answer" had been on the printouts that I'd been using for years. In a nutshell, it was simply the test of signifiance for the group partial regression weights in a full model. An example of a solution for this problem was taken from Williams (1979).

Table 2 is taken from Williams (1974b, p. 104 and 109). In Table 2, X_1 is a binary variable for membership in group 1, X_2 is a binary variable for membership in group 2 and X_3 is similarly a binary variable for membership in group 3 and X_4 represents a pretest score; the Y value represents a posttest score.

Table 2
Data for the Analysis of Covariance

	· · · · · · · · · · · · · · · · · · ·			
. (2, Y	$\mathbf{x_1}$. The second $\mathbf{x_2}$	2	X ₃	X ₄
35	ya i spenilo aksam k	0 >	2	√‱.12
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25	en de la grande de	1	0	12
36	0	1	0	17
25	• • • • • • • • • • • • • • • • • • •	1	0	22
31		1	0	15
27		0	1	17
35	0	0	1	22
19	0	0	1	10
17	0	0	1	8
32	0	0	1	13

Under the assumption of a single regression line on the covariate (the pretest, X_4) an analysis of covariance can be accomplished with two linear models:

$$Y = b_0 + b_1 X_1 + b_2 X_2 + b_4 X_4 + e_8,$$
 [16]

and

$$Y = b_0 + b_4 X_4 + e_9.$$
 [17]

In that a large part of the print-out regarding equation 16 is useful, the print-out is reproduced in Table 3.

The usual analysis of covariance can be completed by using:

$$F = \frac{(R_F^2 - R_R^2)/(g - 1)}{(1 - R_2^2)/(N - C - g)} = \frac{(.61959 - .47476)/2}{(1 - .61959)/11} = 2.09,$$

which for df = 2, 11, p > .05.

In equation 16 the X_3 variable has been omitted. Thus $b_1 = \overline{Y}_1$ adj - \overline{Y}_3 adj and $b_2 = \overline{Y}_2$ adj - \overline{Y}_3 adj. To find the adjusted means, the following equations can be used:

$$\overline{Y}_3$$
adj = $b_0 + b_4 X_4 = 15.36 + .76(15) = 26.76;$

$$\overline{Y}_1$$
adj = b₁ + Y₃adj = 5.52 + 26.76 = 32.28; and

$$\overline{Y}_2$$
adj = b₂ + Y₃adj = 3.20 + 27.76 = 29.96.

The adjusted values agree with those originally given by Williams (1974b, p. 106), though the method shown here is simplified somewhat.

More importantly, the standard error of the regression coefficients corresponding to X_1 and X_2 are respectively equal to the standard errors for comparing \overline{Y}_1 adj to \overline{Y}_3 adj and \overline{Y}_2 adj to \overline{Y}_3 adj. Thus, the computed t values given in Table 3 are directly usable in whichever multiple comparison procedure the researcher prefers. The use of Dunnett's (1955), Tukey's (1953), Dunn's (1961) and Scheffe's (1959) tests are described in a regression format using computed t values in Williams (1976, 1980). Were there interest in comparing \overline{Y}_1 adj to \overline{Y}_2 adj, a model of the form:

$$Y = b_0 + b_1 X_1 + b_3 X_3 + b_4 X_4 + e_8$$
 [18] could be used, with focus on the computed t value for the X_1 variable.

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		P.	Print-Out for Equation 16	quation 16	e e e e e e e e e e e e e e e e e e e		
Variable	Mean	Standard Deviation	Correlation X vs Y	Regression Coefficient	Std. Error of Reg. Coef.	Computed T Value	
4	15.00	5.82	0.689	0.76	0.22783	3.33582	
1	0.33	0.48	0.039	5.52	2.73396	2.01905	
2	0.33	0.48	0.398	3.20	2.92653	1.09345	
Dependent Y	23.66	6.12		eduuri Palaini Palaini	o in .		
INTERCEPT	15.36			i de la companya de l	9		
MULTIPLE CORRELATION	LATION	0.78714					
STD. ERROR OF ESTIMATE	ESTIMATE	4.26230		11 0 25,			
MULTIPLE CORRELATION SQUARED	LATION SQUA	VÆD	0.61959		We Sire		
ONE MINUS MULTIPLE	TPLE CORREL	CORRELATION SQO.	0.38041				
		Analysis	of Variance fo	Analysis of Variance for the Regression			
Source of Variation	ation	Degrees Of Freedom		Sum of Squares	Mean Squares	F Value	
Attributable to Regression Deviation from Regression Total	o Regression Regression	on 33.	୍ ଟ ୍ର	325.49 199.84 525.33	108.497 18.167	5.972	

f course, multiple covariates and/or more complex comparisons can be noncorporated; multiple covariates can be incorporated without adding too uch complexity to the solution. The remarkable thing is that the solution to multiple comparisons for the analysis of covariance is easily achieved.

Multiple Comparisons in Repeated Measure Designs

Again, the impetus (to me) for interest in multiple comparisons in epeated measures designs in general, and treatments x subjects designs in particular comes from students. Students would ask, "O.K., so now we can do a treatments x subjects design by regression. How do we run multiple comparisons?" Since they asked the question long before I had any suitable answer, a question might be asked, "What answer did I give?" To quote both the famous and infamous (e.g. Steve Martin and John Mitchell), "I forgot." Considering that that answer can be as simple as, "It's right there on your printout," I won't dwell anymore on why it took so long.

Multiple Comparisons for Treatments X Subjects Designs

To consider multiple comparisons for treatments x subjects designs

(or repeated measure designs) an example taken from Chapter 7 of

Milliams (1974b, p. 56) is used; see Table 4.

and now and impended alable 4 violents and reserves exercises

Three Treatment Methods of Paired-Associate Learning ration with Educable Mentally Retarded Subjects

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The information in Table 4 can be placed in a tabular form suitable for use in regression format; see Table 5.

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The values in Table 5 are defined as follows:

Y = the criterion score;

 $X_1 = 1$ if the score corresponds to Treatment 1, 0 otherwise;

 $X_2 = 1$ if the score corresponds to Treatment 2, 0 otherwise;

 $x_3 = 1$ if the score corresponds to Treatment 3, 0 otherwise;

 $X_4 = 1$ if the score is obtained from Subject 1, 0 otherwise;

 $X_5 = 1$ if the score is obtained from Subject 2, 0 otherwise;

 $X_6 = 1$ if the score is obtained from Subject 3, 0 otherwise;

 $X_7 = 1$ if the score is obtained from Subject 4, 0 otherwise;

 $x_8 = 1$ if the score is obtained from Subject 5, 0 otherwise;

 $X_9 = 1$ if the score is obtained from Subject 6, 0 otherwise;

 $x_{10} = 1$ if the score if obtained from Subject 7, 0 otherwise;

 $X_{11} = 1$ if the score is obtained from Subject 8, 0 otherwise;

 $X_{12} = 1$ if the score is obtained from Subject 9. 0 otherwise;

 $X_{13} = 1$ if the score is obtained from Subject 10, 0 otherwise; and

 X_{14} = the sum of the criterion scores for each subject separately. A full model for this data could be given as:

 $Y = b_0 + b_1 X_1 + b_2 X_2 + b_4 X_4 + b_5 X_5 + b_6 X_6 + b_7 X_7 + b_8 X_8 + b_9 X_9 + b_{10} X_{10} + b_{11} X_{11} + b_{12} X_{12} + e_{10};$ [19] an alternative model would be:

 $Y = b_0 + b_1 X_1 + b_3 X_3 + b_4 X_4 + b_5 X_5 + b_6 X_6 + b_7 X_7 + b_8 X_8 + b_9 X_9 + b_{10} X_{10} + b_{11} X_{11} + b_{12} X_{12} + e_{10}.$ [20] See Table 6 for a printout using equation 19.

From Table 6, it can be seen that t_1 = 1.10362 and t_2 = 4.59846; that t values are respectively the tests regarding comparing \overline{Y}_1 to \overline{Y}_3 and \overline{Y}_2 to \overline{Y}_3 , taking into account that the subjects serve as their own controls. A similar printout could be generated using a model corresponding to equation 20. Values from this printout show t_1 = -3.49484, t_3 = -4.59847; these t values correspond to comparing \overline{Y}_1 to \overline{Y}_2 and \overline{Y}_3 to \overline{Y}_2 . Also, the corresponding means are \overline{Y}_1 = 13.20, \overline{Y}_2 = 17.00 and \overline{Y}_3 = 12.00. These computed t values should be compared to an appropriate multiple comparison table for significance.

Output of Full Model for Ireatments X Subjects Design

0.4.	Se ta	0.11210 0.46710 0.33690 0.23781	-0.07927 -0.47562 -0.15854	-0.27/45 0.03964 -0.09909 0.31708	100 m 100 m	6.71 1.34 2.7	a. Ne.		* . *		en e	F Value	10.11102
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	Regression Coefficient	1.19998 4.99997 5.66663	4.00001 -1.3333 -7.99992 -2.66665	-4.66664 0.66668 -1.66665 5.3332			•				Analysis of Variance for the Regression	Sum of Squares	657.46021 106.40308 763 86378
	Correlation X vs Y	-0.12145 0.41105 0.39195	0.28185 -0.07046 -0.51085	-0.2966 -0.06166 -0.09248 -0.36993					0.86070	0.13930	Analysis of Va	Degrees Of Freedom	11 18 20
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The solution just given in the last section presumed that each subject (except one) is separately coded using a binary coding scheme. Clearly, if the number of subjects is at all large, the coding procedure described in Williams (1977b) and using:

 $Y = b_0 + b_1 X_1 + b_2 X_2 + b_{14} + e_{10}$ might be preferrable. However, one difficulty with using this shortcut procedure is that the standard error of the regression coefficients for \mathbf{X}_1 and \mathbf{X}_2 are too small due to the degrees of freedom, as generated by the computer program, not being accurate for deviation from regression. These t values could be adjusted by multiplying by an appropriate constant. The appropriate constant is: c = 1where $MS_{W_{21}}$ is the mean square within (or deviation from regression) for equation 21 and ${
m MS}_{
m W19}$ is the mean square within for equation 19. The MS $_{W_{21}}$ is 4.09225 and MS $_{W_{10}}$ is 5.91125. Thus, c = .83203. The values generated by equation 21 for t_1 and t_2 (comparing \overline{Y}_1 to \overline{Y}_3 and \overline{Y}_2 to \overline{Y}_3) are t_1 = 1.32641 and t_2 = 5.52678. Multiplying t_1 and t_2 by c yields corrected t_1 = 1.10361 and corrected t_2 = 4.59845, within rounding error of the values found earlier. Of course, ${\rm MS}_{\rm wig}$ would not be available were the researcher using the shortcut method. However, $\frac{SS_{w}}{N-S-n+1}$ where N is the total number of scores, S is the number of subjects and g is the number of groups. The denominator can also be found as (S-1)(g-1).

Repeated Measures Designs

Multiple comparisons also can be relatively routinized for large data sets involving repeated measures. Williams and Williams (1984) showed

research application of a hypotheses testing process for k groups easured at three times for large N. More recently, they showed in press) the same solutions to the problem done earlier in Williams 1980); a 3 x 4 repeated measure design with five entries per cell was adde to show a problem that was not solvable in a regression format; fortunately (or unfortunately) a solution was found, so the chapter was entitled, "Problems less amenable to a regression solution." In applying this solution to the larger data set, two progressively easier solutions were found; the preferred solution (i.e., easiest to accomplish) is embarrassingly close to a simple Bottenberg and Ward/Ward and Jennings (1973) solution.

Perhaps the point of all of this is to give some comfort to those who have struggled within the use of regression as a technique to address research questions, particularly as they look over their shoulders and think they may never master the process. Insofar as I might be seen as one who has mastered this process, let me point out, I'm still learning!

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The Effect of the Violation of the Assumption of Independence When Combining Correlation Coefficients in a Meta-Analysis

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Susan M. Tracz

California State University, Fresno

Patricia B. Elmore

Southern Illinois University, Carbondale

Meta-analysis is a technique for combining the summary statistics from viously conducted research studies. Pioneered by Gene V Glass (1976) a-analysis gives not only an indication of the direction of the results of studies, but provides an index of the magnitude of the effect as well. ta-analyses are reported in terms of mean effect size, ES. There are two pes of effect sizes. An experimental effect size is the mean of the experintal group minus the mean of the control group divided by the standard viation.

$$ES = \frac{\chi_E - \chi_C}{S_\chi},$$

lile a correlational effect size is simply a correlation coefficient,

ES = r.

Paper presented at the American Educational Research Association, Chicago, April 1985

Meta-analysis has been further refined by Hedges (1983), who has been developing techniques for using effect sizes as data points and then fitting regression models. The focus of this paper, however, will be the use of correlation coefficients in meta-analyses and the effect of the violation of the assumption of independence in these analyses.

The second se

A necessary assumption for the results of statistical analyses to be tenable is independence. All inferential statistical techniques require independence of observations. By independence is meant that the probability of including one subject or data point will in no way affect the probability of including any other subject or data point. Another way of defining independence is to say that the value of a variable for a subject is not predictable from the value of a variable for any other subject.

So far independence has been defined in reference to primary studies perform by researchers who draw a random sample of subjects, measure the subjects on variables of interest, and calculate statistics from the measured data using their hypothesized models. The meta-analysts, on the other hand, draw a sample of studies usually from journal articles, record the numerous statistics reported in each study, and calculate a statistic based on effect sizes or a meta-statistic from a data set of simple statistics. When jumping from the level of individual studies to combinatory techniques, studies parallel subjects and simple statistics parallel observations on variables. In the framework of combinatory methodology, then, independence means that the value of any statist which is included should in no way be predictable from the value of any other included statistic.

The typical study which is chosen for inclusion in a meta-analysis, however will yield more than one effect size or simple statistic. When the meta-analyst uses all the statistics available in a particular study to calculate the mean

size, the assumption of independence is violated. Landman and Dawes (1982) : five ways in which the assumption of independence can be violated in metaes. These five types of violations are as follows: av total be to the second and the second and the second are the second and the second are the second and the second are the second are

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"1) Multiple measures from the same subjects.2) Measures taken at multiple points in time from the

3) Nonindependence of scores within a single outcome

Nonindependence of studies within a single article, . . .

5) Nonindependent samples across articles" (pp. 506-507).

Kraemer (1983) specifically provides the caveat that "only one effect size tudy can be used to ensure independence" (p. 99) in meta-analyses. This that the ratio of effect sizes to studies in a meta-analysis should be n order to avoid violating this assumption. However, even a cursory review iblished meta-analyses reveals that the assumption of independence is, in , seldom met.

pose

The purpose of this study was to determine the effect of the violation the assumption of independence on the distribution of r and the distribution Fisher's Z. In this Monte Carlo simulation the following four parameters were ed with the values specified:

N - the sample size within a study (20, 50, 100),

p - the number of predictors (1, 2, 3, 5),

rho(1) - the population intercorrelation among predictors (0, .3, .7),

rho(p) - the population correlation between predictors and criterion (0, .3, .7).

Predictor and criterion variables were generated to conform to all possible combinations of the parameters specified above and then correlated. The main parameter of interest was rho(i), since it was the index of nonindependence when it assumed a nonzero value in the multiple predictor cases. When only one predictor was used or when the intercorrelation among predictors, rho(i), equaled zero, then the assumption of independence was not violated.

In this study dependent and independent correlations were generated between criterion and predictor variables. The values of the parameter p, the number of predictors, were one, two, three, and five, and path diagrams for each case appear in Figures 1 through 4 respectively. In these diagrams the G variables are the common generating variables used along with error to form the X variables or predictors, which are in turn combined along with error to produce the Y or criterion variables. The arrows between variables indicate the relationship among the endogenous variables. The associated lower case letters are the standardized regression coefficients for path analysis. The arrows which are not

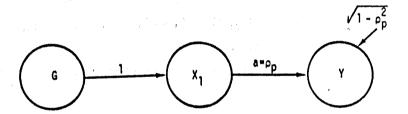


Figure 1. Path diagram for the one predictor case.

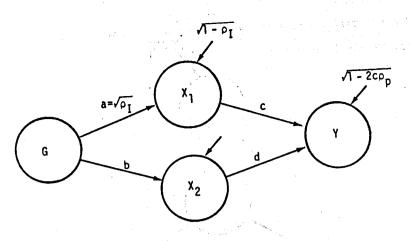


Figure 2. Path diagram for the two predictor case.

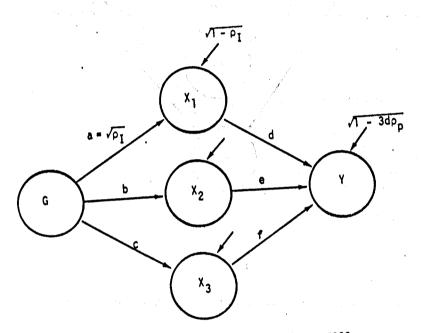


Figure 3. Path diagram for the three predictor case.

 $\begin{array}{c} x_1 \\ x_2 \\ y \\ y \\ x_3 \\ y \\ y \\ x_4 \\ x_5 \\ \end{array}$

Figure 4. Path diagram for the five predictor case.

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tilled i <mark>12</mark>8

nected indicate exogenous variation, and those coefficients are given as well.

The following algorith derived by Knapp and Swoyer (1967) was used to erate correlated vectors of numbers: $Y = aX + \sqrt{1 - a^2}Z^{-1}$

$$y = aX + \sqrt{1 - a^2}Z$$

ere X = a vector of randomly chosen numbers from the standard normal distribution,

- Z = another vector of randomly chosen numbers from the standard normal distribution, and
- a = the desired correlation between X and Y.

In the unique one predictor case, the intercorrelation among predictors ould not be varied since only one predictor was present. Therefore, independence kists in this case. Here the X1 vector was set equal to G, a vector of randomly nosen standard normal deviates, so the path coefficient between G and X1 is one. he path coefficient between X1 and Y, a, was set equal to the population correlation etween predictors and criterion, rho(p). Since a = rho(p), the error coefficient for Y was $\sqrt{1-a^2}$ or $\sqrt{1-\text{rho}(p)^2}$. The Y vector was then created as follows:

$$Y = aX1 + \sqrt{1 - a^2}Z$$

where Z = a vector of randomly chosen numbers from the standard normal distribution. The vectors for X1 and Y were then correlated.

A different procedure was used for data generation in the multiple predictor cases. In Figure 2, path coefficients a = b and c = d. In Figure 3, a = b = cand d = e = f. In Figure 4, a = b = c = d = e and f = g = h = i = j. In these three diagrams the correlations between any two predictors is equal to the product of the path coefficients connecting those two predictors with the generating variable or the quantity, a^2 , since all the coefficients between generating variables and predictors are equal. For the correlation between two predictors to equal rho(i), the path coefficient, a, was set equal to $\sqrt{\text{rho(i)}}$. Then all the X vectors were generated as follows:

$$\chi(i) = \sqrt{aG} + \sqrt{1 - aZ(i)}$$

Where X(1) = a vector of values for a predictor and i assumes incremental values
for vectors from one to p, the number of predictors,

- a = rho(i) = the population intercorrelation among predictors,
- Z(i) = a vector of randomly chosen standard normal deviates and i assumes incremental values for vectors from one to p, the number of predictor

The following points concern the generation of the Y vectors. First it should be noted that each Y is a linear combination of the p predictors plus error. The weight of that combination is c in Figure 2, d in Figure 3, and f in Figure 4. Second, it should be noted that correlation coefficients can be reconstructed from the standardized regression coefficients in a path diagram. In Figure 2, the correlations between the two predictors and the criterion can be reconstructed as follows:

$$r_{yx_1} = c + abd$$

but since c = d, and $a = b = \sqrt{rho(i)}$, the correlation between Y and any predictor X(i), can be written as follows:

$$r_{yx_4} = c + P(1)c = c(1 + P(1)).$$

Also since r_{yx_1} is an estimate of rho(p), that value can be substituted into the equation so that it can be solved for c as follows:

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$$\rho(p) = c(1 + \rho(1))$$

$$c = \frac{\rho(p)}{1 + \rho(1)}.$$

In Figure 3 in parallel fashion, the correlations between the three predictions and the criterion can be reconstructed as follows:

r_{yx1} = d + abe + acf,

ryx2 = e + bcf + bad.

since $a = b = c = \sqrt{rho(i)}$, and d = e = f, the correlation between Y and any dictor, X(i), can be written as follows:

The second second

$$r_{yx_i} = d + \rho(i)d + \rho(i)d = d(1 + 2\rho(i)).$$

so since r_{yx_i} is an estimate of rho(p), that value can be substituted into the uation so that it can be solved for d as follows:

$$\rho(p) = d(1 + 2\rho(1)).$$

$$d = \frac{\rho(p)}{1 + 2\rho(1)}.$$

In Figure 4 the last obvious parallel exists. The correlations between the ive predictors and the criterion can be reconstructed as follows:

 $r_{yx_1} = f + abg + ach + adi + aej$.

 $r_{yx_2} = g + baf + bch + bdi + bej,$

 r_{yx_3} = h + caf + cbg + cd1 + cej,

 $r_{yx_{\Delta}} = 1 + daf + dbg + dch + dej,$

ryx5 = j + eaf + ebg + ech + edi,

but since $a = b = c = d = e = \sqrt{rho(1)}$, and f = g = h = 1 = j, the correlation between Y and any predictor, X(i), can be written as follows:

and any predictor,
$$X(i)$$
, can be written as
$$r_{yx_i} = f + \rho(i)f + \rho(i)f + \rho(i)f + \rho(i)f = f(1 + 4\rho(i)).$$

Again r_{yx_i} estimates rho(p) so with the appropriate substitutions the solution for f is as follows:

$$\rho(p) = f(1 + 4\rho(1)),$$

$$f = \frac{\rho(p)}{1 + 4\rho(1)}.$$

So far in generating the Y variables in the two, three, and five predictor cases, the weights of the combinations, c, d, and f, respectively, have solutio But in each case a weight for the error term is needed. In the Knapp and Swoye algorith, the value a^2 can be viewed as r^2 , the amount of variance accounted for so $1-a^2$ is the amount of variance not accounted for and $\sqrt{1-a^2}$ is the weight the error vector, Z.

In the three multiple predictor cases studied here, formulas for the R² val

$$R_{y\cdot 12}^{2} = c \rho_{yx_{1}} + c \rho_{yx_{2}} = 2c \rho(p),$$

$$R_{y\cdot 123}^{2} = d \rho_{yx_{1}} + d \rho_{yx_{2}} + d \rho_{yx_{3}} = 3d \rho(p),$$

$$R_{y\cdot 12345}^{2} = f \rho_{yx_{1}} + f \rho_{yx_{2}} + f \rho_{yx_{3}} + f \rho_{yx_{4}} + f \rho_{yx_{5}} = 5f \rho(p).$$

The Y variables were generated as follows:

Y =
$$c(X1 + X2) + \sqrt{1 - 2c\rho(p)}Z$$
,
Y = $d(X1 + X2 + X3) + \sqrt{1 - 3d\rho(p)}Z$,
Y = $f(X1 + X2 + X3 + X4 + X5) + \sqrt{1 - 5f\rho(p)}Z$.

Correlations between the criterion variables and each of the predictors were the calculated in the multiple predictor cases

The number of replications was chosen by solving for $n_{\rm r}$ in the formula for the standard error of the mean of the correlation coefficient given below:

$$\sigma_{\frac{1}{r}} = \sqrt{\frac{(1 - \frac{p^2}{r})^2}{\frac{1}{n_s}}}$$

lue for $\frac{1}{r}$ was arbitrarily set at .01, which was deemed sufficiently for precision in this study. In this formula, $\frac{1}{r}$ is the population lation, rho(p), and was set equal to zero. The symbol, n_s , is the sample and was set equal to 20. Substituting these values into the equation ed n_r , the number of replications, to assume the largest value that would estible among the values for parameters, rho(p) and n_s , that were chosen for study. The solution for n_r , the number of replications, was 500. For each combination of N, p, rho(i), and rho(p) and for all r and Z ributions, the means, medians, and standard deviations were calculated.

The means, medians, and standard deviations of the correlation coefficients all values of rho(i), rho(p), and the number of predictors, p, when N=20 are in Table 1. The same information when N = 50 and N = 100 appears in les 2 and 3 respectively.

The means, medians, and standard deviations of the Fisher's Z transformation the correlation coefficients for all values of rho(i), rho(p), and the ber of predictors, p, when n=20 appear in Table 4. The same information n = 50 and N = 100 appears in Tables 5 and 6 respectively.

Inspection of these tables shows that when the population correlation efficient, rho(p), equals zero both the mean of r and the median of r hover ound that value and neither is consistently higher or lower than the other. wever, when rho(p) assumes a nonzero value the median of r is usually larger an mean r. This is because r is a biased statistic and its distribution is egatively skewed when rho(p) is positive. This ordering of the mean and the edian when rho(p) is not zero does not occur in the Fisher's Z distribution.

As N increases both the mean of r and the mean of Z are better estimators f the parameter rho(p). This follows from the Central Limit Theorem. Both the median of r and the median of Z tend to be better estimators of the population

Table 1

Means, Medians, and Standard Deviations for Correlation Coefficients

When N = 20

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$v, i \rightarrow$	er de la v				1 - 2	rho(i) 15 75	act ga	(4) ja	7.4
			0		W g	.3	eren er	1 (32.5)	.7	उम्र
р	rho(p) [,] , , , , , ,	Mdr	SDr	r	Md _r	Sor	33 T 39	Mď	SD
ηa	0	.015	.007	.230		v være	1.00 mg/m 1	err svis	, di	12
	.3	.294	.322	.206						10.00
¥ (4.5)	.7	.690	.706	.126	lei ish b	e valloure di	p bus .	The state of the s	gi e i	
2	.0	.002	.011	.225		007	.223	.002	004	.234
2 78°		.300	.316	.214	.296	.299	.208	.297	.311	.209
	.7	.683	.698	.129	.692	.714	.125	.695	.710	.117
3	0	.001	.003	.230	009	013	.233	.002	007	.228
.d.,	.3	.295	.313	.213	.289	.305	.214	.295	.316	.211 g
1865	.7	b			.686	.703	.126	.687	.703	.126
5	0	002	004	.233	.008	.007	.227	.004	.000	.221
	.3	.293	.309	.216	.307	.320	.208	.292	.303	.202
	.7	ь			b		,	.694	.714	.120
							٠.			0.0

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^aWith one predictor nonzero rho(i) values are undefined.

 $^{^{\}mbox{\scriptsize b}}$ This combination would generate data which are undefined.

Table 2

Means, Medians, and Standard Deviations for Correlation Coefficients

When N = 50

						and the second				
					rt	10(i)				
			0	en	· r	.3 Md,	SD,		.7 ^{Md} r	sD _r
, Y	rho(p)	<u>r</u>	Mdr	SDr		10.00	Y y X	16	- A-1	
a	0	.001 -	.001	.141		gai.			,	
•	.3	.303	.305	.128		gré,				
	.7	.697	.705	.073		.J.	373		,	
_		.005	.000	.142	001	.003	.140	.004	• • • •	.149
2	0	.294	,307	.132	300	.305	.131	.304	.305	.130
	.3		.705	.075	.694	.703	.076	.696	,703	.069
	.7	.697		,139	.007	.003	.145	.001	002	.142
3	0	.002	,001		.295	.300	.130	.295	.300	.136
	.3	.294	.301	.130			.075	.694	.700	.07
	· .7	þ			.696			005	007	.14
5	0	002	001	.143		009		.295		.12
	.3	.299	.303	,129	.300	.305	.129			
	.7	. 6	1		b			.699	.703	

^aWith one predictor nonzero rho(i) values are undefined.

bThis combination would generate data which are undefined.

Table 3

Means, Medians, and Standard Deviations for Correlation Coefficients

When N = 100

						1.5	<u> </u>	** 4		- 1
	the Park State					rho(1)			
	٠.,		0			.3	0		7	
. <u>P</u>	rho	o(p) ř	Md	r ^{SD} r	r	, Md	. SD _r		.7	
1		50 × 50 × 50 × 50	100				100.		a)c≀Md r	SD
	.3	.299	9 .303	.091			esc.	19 0. 198.	0	
	.7	.698	.701	.053					er.	
2	175 ₆ . 0	.004	21.77		008			.00	9 0.012	.097
	.3		.303	* 1000	.304		.0 91		3 .303	2131
,	7		Sala V	.051	699	.703	₀ ∙053	699	703	.048
. 3	1.20	005		.098	.002	.002	1.102	001	.000	.097
	1.00	.301	t to	.092	.302	.305	.092	.300	.302	.088
		3.77 b		.)*	698	.701	.050	.695	°.699	.050
5		002			.003	.001	.100	003	002	.100
		.295	.298	.093	.296	.302	.093	.302	.306	.094
	.7	, b			Ь			.699	.702	.051
										- 4

^aWith one predictor nonzero rho(i) values are undefined.

^bThis combination would generate data which are undefined.

Table 4

Means, Medians, and Standard Deviations for Fisher's Z Transformation
of the Correlation Coefficients When N = 20

						rho(i)				
			0			.3			.7	
Р	rho(p	Z	Md z	SD _Z	7	Md z	SD Z	Z	Md	SD
1 ^a	0 :	.016	.007	.243						
	.3	.317	.334	.233					•	
	.7	.885	.879	.237				. 14		
2	0	.002	.011	.238	004	007	.235	.002	004	.247
	.3	.327	.327	.246	.321	.309	.240	.323	.321	.242
	.7	.873	.864	.242	.890	.895	.241	.893	.887	.230
3	0	.001	.003	.244	009	013	.246	.002	007	.241
	.3	.321	.324	.244	.313	.315	.244	.321	.327	.242
	7.7	b			.879	.874	.242	.880	.873	.241
5	0	002	004	.246	.009	.007	.240	.004	001	.233
	.3	.319	.319	.248	.334	.331	.240	.316	.313	.231
	.7	ь		•	b			.891	.895	.229

^aWith one predictor nonzero rho(i) values are undefined.

^bThis combination would generate data which are undefined.

Table 5

Means, Medians, and Standard Deviations for Fisher's Z Transformation

of the Correlation Coefficients When N = 50

					and a feet of the	rho(i)	grant agenti	San		n. _w .
			0			.3		and the	.7	in the second
р	rho(p)	Z	Md z	SDZ	Z	Md z	SDZ	√ z	Md z	SD z
1ª	0	.001	001	.144			The mark	termi skietiščinimo z 3 1 5 g.,		
	.3	.319	.315	.144			W .			
	.7	.876	.877	.144		£ 14.	1.8	880L	6	
2	0	.005	.000	.145	001	003	.142	.004	.005	.152
V +	.3	.309	.317	.146	.316	.315	.147	,,, , 32 0	.315	.146
	.7	.877	.877	.145	.870	.873	.147	.873	873	.136
3	0	.002	.001	.141	.007	.003	.148	.001	002	.145
	.3	.309	.310	.146	.310	.310	.145	.311	.309	.152
	.7	b			.874	.874	.145	.870	.867	.149
5	. 0	002	001	.146	006	009	.147	005	007	.144
	.3	.315	.313	.145	,316	,315	.145	.310	.310	.143
	.7	. b			ь			.878	.877	.141

^aWith one predictor nonzero rho(i) values are undefined.

bThis combination would generate data which are undefined.

Table 6

Means, Medians, and Standard Deviations for Fisher's Z Transformation
of the Correlation Coefficients When N = 100

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								gent to talk	1,75	$\frac{1}{(k-1)^{n-1}}$ \mathcal{F}' .
					rl	no(i)				
			0			.3			.7	es d
P	rho(p)	7	Mdz	SDz	7	Mdz	SDz	7	Mdz	SD _Z
1 ^a	0	.008	.005	.110		• .			* , (C)	pu simbe
	.3	.311	.313	.101					€+1 = 5 °°2	- 5g3
	.7	.870	,869	.102						
2	0	.004	.003	,101	008 -	009	.102	.009	.012	.098
	.3	.309	.312	.100	.317	.318	.101	.316	.313	.098
	.7	.874	.875	.100	.873	.872	.104	.872	.874	.094
3	0	005	009	.099	.002	.002	.103	-,001	.000	.098
J	.3	.313	.315	.102	.315	.315	.103	.313	.312	.097
	.7	ь	-		.870	.869	.097	.863	.865	.097
e	_		002	.100	.003	.001	.101	003	002	.101
5		.308			.309	.311	.102	.315	.316	.105
	.3 .7	.300 b	,550	*	b			.871	.872	.100

^aWith one predictor nonzero rho(f) values are undefined.

bThis combination would generate data which are undefined.

parameter, rho(p), as N increases as well. Both the mean and the median are consistent estimators. It should be remembered here that when r equals zero, Fishe Z also equals zero. However, when r is .3, Z is .31; and when r is .7, Z is .86.

Inspection of the tables shows that there is no discernible trend in mean r, mean Z, median r, and median Z over levels of rho(i) or levels of p. This seems to indicate that nonindependence of the data does not affect the estimation of the population parameter, rho(p). This is, of course, only for the case when the same parameter is being estimated by all the data.

When evaluating the standard deviations they should be referenced to the known expected values in the cases when independence is not violated. For the r distribution, the standard error of r can be found by substituting the values for the parameters used in this study into the following formula:

$$\sigma_r = \sqrt{\frac{(1 - \rho(p)^2)^2}{n}}$$

Therefore, the standard error of r when rho(p) is 0 and N is 20 is approximately .224. The standard error of r when rro(p) is .3 and N is 20 is approximately .204

The standard error of r when rho(p) is .7 and N is 20 is approximately .114. When rho(p) is 0 and N is 50 the standard error of r is approximately .141. When rho(p is .3 and N is 50 the standard error of r is approximately .129. When rho(p) is . and N is 50 the standard deviation is approximately .072. The standard error of r when rho(p) is 0 and N is 100 is .1. The standard error of r when rho(p) is .3 and N is 100 is approximately .091. Finally, the standard error of r when rho (p) .7 and N is 100 is approximately .051.

Inspection of Tables 1, 2, and 3 shows that all the standard deviations are close to their expected values. The largest deviation of the standard deviation from its expected value was .015 and that was in an independent case. This deviation is of no practical concern. There is some improvement as N increases

se standard deviations are consistent estimators, but there are no apparent es over levels of rho(i) or p.

For the Fisher's Z distribution, the values of the standard deviations can und by substituting the values for the parameter used in this study into ollowing formula:

$$\sigma_{z_r} = \frac{1}{\sqrt{N-3}}$$
.

efore, the standard error of Z when N is 20 is approximately .243. The dard error of Z when N is 50 is approximately .146. Finally, the standard r of Z when N is 100 is approximately .102.

Again inspection of Tables 4, 5, and 6 shows that all the standard deviations very close to their expected values. There is some improvement in the estimates increases, but there are no apparent changes over either levels of rho(i) or p.:lusion

The general conclusion, then, is that nonindependence does not affect the imation of either the measures of central tendency or the standard deviations correlation coefficients and for Fisher's Z transformation of the correlation efficients when the same population paremeter is being estimated.

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Time Series Arima Models of Undergraduate Grade-Point Average

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Abstract

The Box-Jenkins approach to time series analysis, a regression method r analyzing sequential dependent observations, was used to select the st appropriate stochastic model for describing undergraduate grade point erages. The technique, applied to approximately a half century of ta from two universities, suggested that the moving average model ovided the optimal fit. Suggestions were made for further exploration GPA data. GPA data.

Whenever a phenomena is observed over time, it is often useful to search for temporal patterns within the data. Economists have studied stock market prices, sociologists have examined population levels, and psychologists have investigated changes in the incidence of depression. For such purposes, a variety of time series analysis procedures have been developed, derived primaril from the theory of multiple regression. These techniques require data gathered from at least fifty time periods (McCleary and Hay, 1980, p. 20). Since archival data covering this many time periods is not as commonly collected in education as in some other fields, these mathematical approaches are not as widely used in educational research. It is the purpose of this paper to illustrate such an application, using undergraduate grade point averages.

Although educational institutions evaluate their students each term, a single group of pupils is not often evaluated fifty times on the same variable; as would be required for a time series analysis. However, a meaningful time and series can be realized by obtaining the average grades given during each of the grading periods across a lengthy time span. For about the last half century, many universities and colleges have adopted a 5-point grading scale, using either the letters A through E or the numbers 1 through 5. Some of the institutions calculated, at each grating period, the average of grades awarded to their students, with the intent of maintaining reasonable consistency in their grading standards both among their departments and across time.

Approximately fifteen years ago, reports began appearing that a conspicious increase was occuring each year in the grading patterns at many institutions (Birnbaum, 1977). Although that pattern appears to have abated during the past few years (Suslow, 1977), grades remain at a noticably higher level than

Time Series Arima Models of Undergraduate Grade-Point Average

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The Box-Jenkins approach to time series analysis, a regression method analyzing sequential dependent observations, was used to select the appropriate stochastic model for describing undergraduate grade point ages. The technique, applied to approximately a half century of from two universities, suggested that the moving average model /ided the optimal fit. Suggestions were made for further exploration iPA data.

oper presented at the American Educational Research Association, Chicago, April,

Whenever a phenomena is observed over time, it is often useful to search for temporal patterns within the data. Economists have studied stock market prices, sociologists have examined population levels, and psychologists have investigated changes in the incidence of depression. For such purposes, a variety of time series analysis procedures have been developed, derived primari from the theory of multiple regression. These techniques require data gathered from at least fifty time periods (McCleary and Hay, 1980, p. 20). Since archival data covering this many time periods is not as commonly collected in education as in some other fields, these mathematical approaches are not as widely used in educational research. It is the purpose of this paper to illustrate such an application, using undergraduate grade point averages.

Although educational institutions evaluate their students each term, a single group of pupils is not often evaluated fifty times on the same variable as would be required for a time series analysis. However, a meaningful time we series can be realized by obtaining the average grades given during each of the grading periods across a lengthy time span. For about the last half century, many universities and colleges have adopted a 5-point grading scale, using either the letters A through E or the numbers 1 through 5. Some of the institutions calculated, at each grading period, the average of grades awarded to their students, with the intent of maintaining reasonable consistency in their grading standards both among their departments and across time.

Approximately fifteen years ago, reports began appearing that a conspicious increase was occuring each year in the grading patterns at many institutions (Birnbaum, 1977). Although that pattern appears to have abated during the past few years (Suslow, 1977), grades remain at a noticably higher level than

and the second and the second and the second

to the increase.

A variety of factors have been suggested to explain the phenomena of tutional grade average fluctuation (Birnbaum, 1977), but there has been k of data that support the proposed explanations. Rogers (1983) ned several independent variables (demographic and economic) for the ibility of explaining temporal variation over an extended time frame, found each of them lacking in explanatory power.

Any "explanation" of a pnenomena implies that the phenomena can be uately described. Hathematical models, and regression models in particular, appropriate for such a description, but an examination of the literature ests that most authors rely solely on visual graphs rather than employing ematical modeling. It was the purpose of this study to use a stochastic series approach to generate mathematical models that might appropriately ribe the entire sequence of grade point data.

Method

)le

Grade point average data were collected from two midwestern universities about a fifty year span. For the first, hereafter called University A, was collected for each year from 1929 through 1982. This data is plotted a time series plot in Figure 1. For the second institution, hereater called versity B, data was collected each year from 1932 to 1982, except for the irs 1943 through 1946, when no data was available. This data is plotted in jure 2.

cedure

These data were analyzed with the time series analysis procedures ought together in 1970 by George E. P. Box and Gwilyn M. Jenkins, in their lume entitled <u>Time Series Analysis</u>: <u>Forecasting and Control</u> (revised

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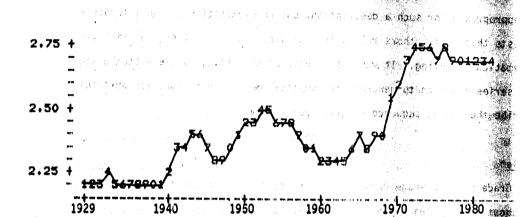


Figure 1. Grade Point Average (GPA) at University A, by year, from
1929 to 1982. (Prior to 1944 the data is for the whole
year; afterward it is for fall term.)

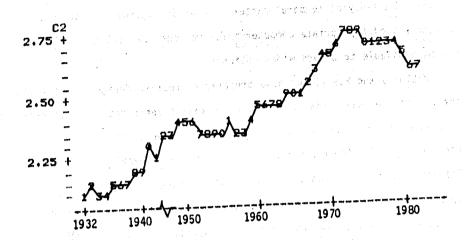


Figure 2. GPA at University B, by year, from 1932 to 1982 (fall term).

Far 1943-1946, data are not available.

edition 1976). These Auto-Regressive Integrated Moving Average (ARIMA) models (often referred to as "Box-Jenkins" models) require a large amount of data. However, when data are collected over an extended time period, as in this study, there is the possibility that the social meaning of the data could change over time. Thus, it becomes difficult to assign the same interpretation to the data at the beginning and end of the series. None-theless, the study of temporal patterns is an intriguing one, and with the development of appropriate computer software, the Box-Jenkins methods have become available to a much wider audience.

McCleary and Hay (1980) have prepared a treatise designed to encourage the use of the Box-Jenkins analysis for social science data, and to explicate strategies for both analyzing the data on the computer and presenting the computer output. Their strategies undergird the analysis in this study. The data was processed on a Harris computer, using MINITAB (Ryan, et al., 1982). Other approaches and other computer programs could have been used, but this was the one available for this project. The reader will need to interpret the methodological procedure of this study in that light.

STATE OF STA

The empirical identification procedures recommended by Box and Jenkins require an analysis of the autocorrelation function (ACF) and the partial autocorrelation (PACF) of the time series. The graphed ACF and PACF for, both of the University time series are shown in Figures 3 and 4. The ACF is a set of correlations, each one of which represents the correlation between the original sequence and itself when lagged

k units. For observations close together, e.g., 1 or 2 lags, we most often find a higher correlation than for observations further apart, as is typifie in Figures 1 and 2, where the correlations are slowly dying out as the lags

Autocorrelations

	-1.0	0 -0.8 -0.4 -0.4 -0.2 10.0 0.2 10.4 nt 0.6 tn 0.8 st 1.0 nt
1 2 3 4 5 6	0.931 0.849 0.753 0.666 0.567 0.484	Canada XXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX
7 8 9 10	0.392 0.312 0.221 0.119	XXXXXXXXX Sant Labra ogress and XXXXXXXX Sant Labra ogress and XXXXXXX XXXXX Sant Labra ogress and XXXXXXX XXXXX XXXXXX XXXXXXXXXXXXXX
11 12 13 14	0.026 -0.042 -0.084 -0.112 -0.101	XX XX XXX XXXX AXXX
16 17	-0.060	XXX XXX

Partial Autocorrelations

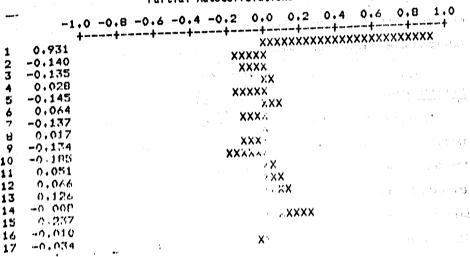


Figure 3. Estimated ACF and PACF for GPA. University A.

increase. This dying out phenomena is a consequence of the fundamental tenent of the ARIMA model, namely that the effect of any given input to the system declines over time. (Note that this is just the opposite of a time series of a bank savings account where, assuming a constant interest rate, the compounded interest from the first dollar invested is always larger than that from any subsequent dollar invested.) When the data is properly modeled, the residuals (errors resulting from the model) should be randomly distributed, and thus yield an ACF with with values that are all statistically non-significant. The goal of the Box-Jenkins approach is to find such a model.

The Box-Jenkins approach is a three stage procedure to build a model, ate consisting of Identification, Estimation, and Diagnosis. Each of these will be illustrated in the following analysis. The cycle iterates until an interpretable solution is found.

University A

Identification.

An examination of the ACF of the raw data (Figure 3) shows that the ACF falls to zero slowly, indicating that there is a strong systematic trend in the data. The most common method for removing this trend is to transform the data by replacing each observation with the difference between it and the preceding observation. When this differencing transformation is complete, the ACF is again computed. Figure 5 shows the ACF for the differences. The values are much smaller, indicating almost random data. However, there are some spikes, which may be due to sampling error or to some systematic process, so further analysis is required.

The PACF is interpreted similar to the ACF, except that each value is the correlation between observations \underline{k} units apart \underline{after} the correlation at

Autocorrelations

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0.174		XXXXX							
0.129 0.093	1	XXXX	123						
0.060		XX							
0.032	•	XX					•		

Partial Autocorrelations

Figure 4. Estimated ACF and PACF for GPA. University B.

Autocorrelations

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. 3	0.046	TO CONTRACTOR OF CARE OF SERVICE SERVICES.	XX
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. 8	-0.065		XXX 555 655 1.6610
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13	-0.104	and the second of the second o	Ø.174 XXXX
14	-0.265		XXXXXXX
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17	-0.035		XX

Partial Autocorrelations

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ذ	0.071	XXX	A (64 🗗
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G	0.158	XXXXX	1.11
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īĭ	-0,100	ZXXX	
12	0.068	XXX	Ô
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14	-0.133	^XXX	
15	-8.001	^% %;	• O ~
16	-0.162	XXXXX	
17	0.043	^^^^ XX	
1/	V+V43	A → A →	

Figure 5. Estimated ACF and PACF for first differences. University A.

intermediate lags has been controlled or "partialled out". The PACF in Figure 3 shows a single spike, which may be the result of what is called a moving average (MA) component. This moving average component can be conceptualized as a random "shock" which is added to each observation to obtain the predicted value for the next observation.

Company of the state of the sta

The distinguishing characteristic of a moving average process is the finite duration of the shock. The shock persists for q observations and then is completely suppressed (McCleary and Hay, p. 61). Such a "shock" might be the result of the new grades that are added each term for each particular student. Since the majority of students will leave the institution after four years, the impact of any particular student will vanish when that individual leaves.

From the ACF and PACF we can now tentatively "identify" the model as an ARIMA (0, 1, 1). The zero indicates that there is no auto regressive (AR) term, the middle 1 indicates that differencing is to be used (this is the Integrative (I) term), and the last 1 indicates a moving average (MA) term. Estimation.

When the estimates of the parameters were computed, it was found that the (0, 1, 1) model produced a t-value of only 1.23 for the MA term. Since this value was not statistically significant at the .05 level (nor anywhere near there), the model was rejected, and the procedure returned to the identification stage.

Identification.

It might be useful at this point to emphasize that since the estimated ACF and PACF are based on very small samples, they are subject to relatively large sampling errors. Consequently, any identification is very tentative.

Because the ACF and PACF for first differences appeared rough, it seems appropriate to take second differences, i.e., differences between the difference scores. Figure 6 shows the resulting ACF and PACF. They appear more interpretable, suggesting a (0, 2, 1) model. An examination of Figure also suggested that the variance was not constant across time. To attempt to correct this, a logarithmic transformation of the data was performed.

Estimation.

Table 1 shows the results of estimating the (0, 2, 1) model. The movin average parameter of .9767 satisfies the stationarity requirement that its absolute value be less than 1.0, and is also statistically significant at less than the .05 level.

Diagnosis.

The simplest diagnostic procedure is to compare the results of the given model and alternative models. In this way, it can be shown that a particular model is optimal in that neither a simpler nor a more complex model will suffice. The simpler model (0, 1, 1) was already shown to be inadequate. The more complex model (0, 2, 2) yielded a statistically insignificant second MA term, so it was rejected. The (1, 2, 1) model was also tested, but the AR term was insignificant. Thus, the ARIMA (0, 2, 1) model was accepted as the "best" fit.

The equation generated by this procedure can be conveniently written in the following form: $(1-B)^2y_t = (1-.9767B)a_t$ where B is the backshift operator, and a_t is the random-shock element (McCleary and Hay, (1980), p. 4664). The backshift operator is defined as $By_t = y_{t-1}$ and follows the usual algebraic rules. The operator (1-B) represents first differences and $(1-B)^2$ represents second differences.

Autocorrelations

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11 12 13 14	-0.085 0.143 0.037 -0.265	*** ***** ** ******	(1995년 - 1995년 (1996년 1996년 - 1996년 - (1996년 - 1996년 - 1996 - 1996년 - 199
15 16 17	0.217 -0.097 0.036	yxxxxx xxy xx	

Partial Autocorrelations

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567	-0.318 -0.139 -0.131	^^^^^XXX	A.3
9 9	-0.287 0.236	xxxxxx::	
10 11	-0.073 -0.179	**************************************	en de la companya de
12 13	0.039	X	the second secon
14	-0.072		
15 16 17	-0.028 -0.206 0.021	xxxxî; Xx	

Figure 6. Estimated ACF and PACF for second differences. University A.

Table 1. Parame	eter estimates for the	ARIMA (0, 2,	l) model. University A. ****
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FINAL ESTIMAT NUMBER TY	E5 UF PARAMETERS PE ESTIMATE	inakanan p	COTAGE ALBERT E(0.0) C -RATIO ELAN SE FRONCE 22.24 OFF.0
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		stronger in April 1984	the place

Table 2.	Parameter es	stimates for the	ARIMA (0, 2	- 21 mail - 1 - 3	University B.
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FINAL E	BTIMATES OF	PARAMETERS		1918 - C	· 0
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318.0- 318 MA 2 -0.5302 0.1220 DIFFERENCING. 2 REGULAR
RESIDUALS. 88 = 0.0429018 (BACKFORECASTS EXCLUDED)
DF = 43 MS = 0.0009977

NO. OF OBS. ORIGINAL SERIES 47 AFTER DIFFERENCING 451

The state of the s

The random shock element a_t is the stochastic component in the equation. the ARIMA model this moving average component can be shown to be matheically equivalent to the exponentially weighted average of all previous ervations (Pankratz, 1983, p. 49, 109; McCleary and Hay, (1980), p. 63).

University B

ntification.

An examination of the estimated ACF and PACF of the raw data (Figure 4) gests that this data is also non-stationary and needs to be differenced. single spike on the PACF suggests a (0, 1, 1) model. imation.

The (0, 1, 1) model produced an estimate of the Moving Average parameter n a t-value of .23. Since this was far from statistical significance, ifications needed to be made. Second differences were used, since the a appeared to approximate a quadratic trend. The (0, 2, 1) model produced arameter with a t-value of 11.12, which was highly significant.

The model was first diagnosed by comparing it with a more complex model. ordingly, a (0, 2, 2) model was tested. It produced significant t-values both MA parameters, as shown in Table 1. To compare the two models, the n squares of the residuals was computed. The (0, 2, 1) model yielded = .0011274, while the (0, 2, 2) model yielded MSR = .0009977. Finally, 1, 2, 2) model (yet more complex) was tested, but it yielded MSR = 11641. Consequently, the (0, 2, 2) model was favored, since it yielded smallest MSR.

The ACF and PACF for the Residuals of model (0, 2, 2) are shown in ture 7. No spikes are shown at lag 1 or any other lags. The residuals ear to meet the diagnostic criteria, so the model is accepted.

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			and the state of t

Figure 7. Estimated ACF and PACF for residuals from Arima (0, 2, 2) model. University B.

The model can be conveniently written as $(1-B)^2y_t = (1-1.1475B + .5302B^2)a_t$.

Conclusion

gendy of Syl

This paper has suggested that meaningful mathematical models can be created to describe the time series of changes in the yearly grade point average at a university. The models are very tentative, partly because of the small number of available observations and also because of their relative complexity.

While this paper has not answered the questions about the so-called "grade inflation," it has indicated that a mathematical description of the time series of grades is sufficiently complex to suggest that no simple answer may suffice. The data is unstationary, as shown by the need for differencing. It further appears to be best modeled by an approach that postulates random shocks that persist for only a finite time, yet each of which can be represented as an exponentially weighted average of all previous observations. This perhaps reflects both the influx of new students and the persistent effects of traditional grading practices.

Data for this study was available for only two institutions of higher education, so the generalizability of the results is limited. Studies with data from other institutions would serve to indicate the existence of general patterns across institutions.

Birnbaum, R. (1977). Factors relating to university grade inflation. C. B. Journal of Higher Education, 48, 519-539.

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Notes and Tables to Accompany the Presentation:

Multiple Regression Analysis with

Dichotomous Outcome Variables: Issues and Examples*

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Ric Brown

California State University, Fresno

OVERVIEW

The purpose of this 'applied' presentation is to demonstrate the use of multiple regression analysis in situations where the outcome variable is dichotomous and the predictor variables are intervally scaled. The more common procedure in this situation is discriminant function analysis. However, Cohen and Cohen (1975) state:

"A few moments of reflection will make it apparent that for the special case where two groups are to be discriminated.... the analysis reduces to a single MRC for a single dichotomous Y (which can be coded 1 - 0, or with any other pair of different values). The MRC analysis is mathematically and statistically identical with a CA when p=1; hence, it is identical with a DA for 2 groups. R\$\frac{1}{2}.12...k equals the (sole) R\$\frac{1}{2}(=R\$\frac{1}{2}_1) and the multiple regression equation is proportional to the discriminant function and hence perfectly correlated with it(p.442)."

Mathematical formulations can be found in Tatsouka (1975).

Issues regarding the use of the general linear model (discriminant function or multiple regression) with qualitative variables is beyond the scope of this presentation. Press and Wilson (1978) argue that logistic regression is preferable to discriminant function analysis when one or more of the discriminating variables is qualitative. However, they also state a preference for discriminant analysis estimators "if the populations are normal with identical covariance matrices."

Note: Also see Myers, M., Templer, D., and Brown, R. (1984). Coping ability of women who become victims of rape. <u>Journal of Consulting and Clinical</u>

Psychology, 52 (1), 73-78.

Paper presented at the American Educational Research Association, Chicago, April, 198

The research sought to investigate the coping skills of tape victims to determine if some women may be more vulnerable to rape than others. The study investigated five domains: psychosocial competency, mental health, alcohol and drug use, cognitive resources, and physical ability. Seventy-two rape victims and 72 control women were administered psychometric instruments and a biographi inventory. Information was also obtained from significant others. The stronge domain of prediction was psychosocial competency, with the rape victim scoring lower on measures of social presence, dominance, and assertiveness, and higher on external/social locus of control. A past history of alcohol or drug abuse added to the rape-vulnerability profile. Rape victims were more likely to have a past history of psychiatric hospitalization and suicidal thoughts. They did not differ from control women on the Vocabulary subtest of the Wechsler Adult Intelligence Scale-Revised, but they scored lower on the Achievement via Independence Scale of the California Psychological Inventory. Physical ability attributes were not associated with rape vulnerability (see article).

Points:

1) choice of the stepwise model

BEACH WERE THE FREE A.

- 2) acceptability of the regression approach to journals
- 3) presentation of the data

EXAMPLE 2

The problem of unwed adolescent pregnancy has been studied in the past primarily as a symptom of individual psychopathology. These studies yielded equivocal results. Gradually, the broader social context of pregnant teenagers began to be studied. Past research pointed to the importance of the family contributing to the problem.

The objectives of this study were to investigate whether family variables could discriminate between the families of unwed pregnant and non-pregnant teens All teen subjects met the research criteria of being unwed, under eighteen years of age, enrolled in local high schools, and living with their families of origin Thirty-one pregnant teen families and 28 non-pregnant teen families comprised the study sample. Each subject completed the Moos Family Environment Scale (FE In addition, each parent completed a questionnaire which included a problem checklist, demographic information, questions about the teen's dating behavior and recent family structural changes.

The hypothesis that incongruence of perception and other family adjustment variables could differentiate the two groups was explored. Pregnant teens were found to have longer boyfriend relationships and fewer problems as rated by the parents. Their family's perceptions were more congruent regarding cohesion and mother/daughter interaction, but less congruent in terms of family conflict (tables 1 and 2).

Points:

1) choice of full model

TABLE 1

Means of Variables by Pregnant/Non-Pregnant Groups

Variable	Gr Pregnant (1)	coup gods Non-Pregnant (2)
	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	adore to recept forces
Length of Boyfriend Relationshi	p(mos.) 10.20	3.20 Section approximation of the section of the se
Conflict Incongruence	3.93	2.56
Number of Problems	.8	1.70 grander til grand til Alband de
Control Incongruence	2.6	2.18
Cohesion Incongruence	3.26	4.0
Organization Incongruence	3.6	3.25 Simple of the state
Mother/Daughter Incongruence	28.23	33.0
Family Changes	1.63	1.56
Independence Incongruence	2.93	3.06

Summary Table of the Regression Analysis with Incongruence of Perception and Other Family Variables

intramenta enta litrigia.

	Independent Variables	the raise constitution of the same constitution of the same same same same same same same sam
		of more some livery to
Marining and their Mariana in the	Length of Boyfriend Relationship	7.43
	Conflict Incongruence	28 state v
and which the second	Total Number of Problems	• 20
	Control Incongruence	09
	32 2 . 1	कार अस्ति के देश हैं ते सम्पर्धक के उन्ह ें के सम्पर्धक के अस्ति के स्वाप्तिक के स्वाप्तिक के स्वाप्तिक के स्वाप
	Cohesion Incongruence	.13
	28 s	Femilian of Freshiltens
	Organization Incongruence	08
	The state of the s	Southern implement of the and result.
	Mother/Daughter Incongruence	.21
	The state of the s	conservation of the constant o
	Number of Family Changes	02
		Elimbonic tion income
	Independence Incongruence	
		The second secon

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 $(x_i,y_i) = \frac{1}{2\pi i} \frac{\partial Q}{\partial x_i} (x_i,y_i) \sum_{i=1}^{n} \frac{Q}{\partial x_i} (x_i,y_i)$

p< .01

EXAMPLE :

This study examined the effects of acculturation on adolescent development, specifically focusing on daydreaming as one aspect of coping and adaptation. An investigation of two samples of acculturating (Hispanic and Native American) and acculturated (Caucasian) adolescents revealed two variables that, in combination, significantly differentiated the two groups. These two variables, fear of failure daydreams and distractibility, suggested that acculturating adolescents were more likely to report guilty and fearful daydreaming themes and less likely to report concentration difficulties than their acculturated coparts (tables 3,4 and 5).

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Point Biserial Correlations of Daydreaming Variables with Acculturation Index

, .Variables	Correlation
Frequency with the second	101 10 100 100 100 100 100 100 100 100
Visual Imagery Problem-Solving Daydreams	03
Future in Daydreams Bizarre and Improbable Daydreams Mind Wandering	.06 .04
Achievement-Oriented Daydreams Hallucinatory-Vividness	16 .07 .08
Fear of Failure Daydreams Hostile Daydreams	.33
Guilt Daydreams Boredom	.27 05
Distractability	12

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Table 4

Summary: Table of the Stepwise Multiple Regression Analysis with Acculturation as the Dependent Variable

	Independent Variables	Multiple R	R Square	Change in R Square	Simp
				and the second s	n o ranganga pagaga
	Fear of Failure Daydreams (DM)	.33	.11	.11	
r	•				
	Distractibility (DQ)	.42	.17	.06*	

*Variables beyond this point did not significantly account for additional between group variability (PC<05).

Table '

Acculturating vs. Acculturated Group Means on the Independent Variables

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Variable	Acculturating(1) Mea	ns Acculturated (2
The second secon	the limit with the second	erson in it has broken
Davdreaming Villet	ther Karlan reall that we	
Frequency 40 80 40 1 201	35.38	36.54
Absorption in Daydreaming	52.67	52 96
Acceptance of Daydreaming	30.82	
Positive Reactions	30.59	20.46
Frightened Reactions	38.88	39.64
Visual Imagery	32.76	33.38
Problem-Solving Daydreams	30.03	30.34
Future in Daydreams	30.71	31.96
Bizarre & Improbable Daydreams		41.98
Mind Wandering	32132	30.24
Achievement-Oriented Daydreams		38.86
Hallucinatory-Vividness	40.68	42.30
Fear of Failure Daydreams	34.68	39.48
Hostile Daydreams	34.15	39.24
Guilt Daydreams	41.85	46.18
Boredom	41.32	40.60
Distractibility	36.26	34.66

NOTE: A high score on each daydreaming scale means that respondents disagreed with the scale's major theme. For example, a high score on Fear of Failure Daydreams means that the subject reports few fear of failure daydreams.

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Significant Interaction: I Got What I Needed

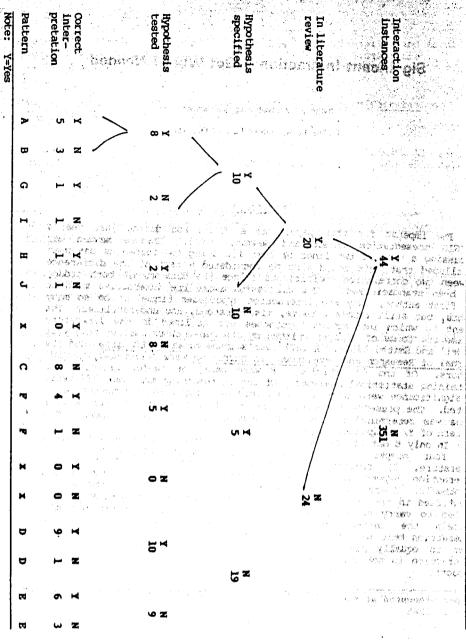
Keith A. McNeil and Gail Smith **Dallas Independent School District**

Background

The impetus for this paper was a discussion during last year's /SIG presentation (Hoedt and Newman, 1984). Isadore Newman was cussing a test of two lines of best fit being considered as one when alluded that this could also be considered a test of the difference ween two correlation coefficients (since the data within both groups been standaridized.) The discussion awoke the interactive mind of first author. Why are interaction hypotheses hinted at on so many onts, but still remain elusive, misunderstood, and underutilized? The ent to which interaction hypotheses are utilized in the literature name the focus of a paper written by the two authors earlier this year Neil and Smith, 1985). A full year's issue of <u>Orban Education</u> and the Irnal of Research and Development in Education were reviewed by the two thors. Of the 57 articles, 38 were essay or review articles not ntaining statistical analyses. Of the 19 remaining articles, 386 tests significance were computed, with only 44 interaction hypotheses being sted. The presence (Y) or absence (N) of each aspect of four crucial ups was determined for each of these 44 interaction instances. The ttern of Y/N responses is presented in Table 1.

In only 5 out of the 44 instances (Pattern A) did the author follow four steps: 1) identify the interaction hypothesis in the terature, 2) specify the interaction hypothesis, 3) test the interaction hypothesis, and 4) correctly interpret the interaction pothesis. There were 8 instances of Pattern C, wherein the author lentified in the review of literature juicy interaction hypotheses, but illed to carry through. Pattern D represents the computer society, derein the canned computer program automatically provides the atteraction test so the author feels obligated to interpret the results. at is equally disturbing is the last two bins, Pattern E. Here iteraction is not discussed until the interpretation stage - food for hought.

aper presented at the American Educational Research Association, Chicago, \pril, 1985



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Review of Multiple Linear Regression Viewpoints for Applied Interaction Studies

Interaction hypotheses can easily be tested within the Multiple Linear Regression (MIR) approach, and there has been a history of MIR being taught alongside "complex behavioral science models incorporating interaction and non-linear variables (Kelly, Beggs, and McNeil, 1969; interaction and non-linear variables (Kelly, Beggs, and McNeil, 1969; fraser, 1979; Bottenberg and Ward, 1963). It was therefore predicted that a higher percentage of interaction hypotheses would appear in Multiple Linear Regression Viewpoints, (the journal of SIG/MIR) than in the two journals previously reviewed.

When the predictors were used to predict the criterion

*for the experimental and control groups separately,
apparent differences were found in the two regression
equations. It was these differences that led to the
present consideration of the interaction of the
predictors with experimental condition (Group) as a
way of exploring the differences statistically.

(pinero, 1976)

So begins one of the few research studies which tests an interaction hypothesis in a meaningful way. All issues from 1975 through 1980 were reviewed. Only nine applied studies were found, with 49 of the 506 tests of significance involving interaction. Of the five studies which did consider an interaction hypothesis, two studies fit Pattern B (10 consider an interaction instances), one Pattern F (28 interaction instances), and two interaction instances), one Pattern F (28 interaction instances), and two interaction instances). In no case did the researcher include all four of what we consider to be crucial steps. Additionally, the percentage of interaction hypotheses is lower in Viewpoints than in the two applied education journals discussed earlier. This finding is particularly disconcerting because much has been written in Viewpoints about interaction and how easily one can test it within the MIR about interaction and how easily one can test it within the MIR reinforce these interaction notions. Fraser (1979) provides a comprehensive approach to research with MIR. Researchers who haven't interacted within the last five years ought to reread the article.

Review of Multiple Linear Regression Viewpoints for Interaction Comments

Why so few researchers test interaction questions remains a puzzle. All canned ANOVA computer programs routinely provide a test for interaction. All stat texts discuss the concept, most in a negative light though. (The Kelly, Beggs, and McNeil (1969) text had the audacity to place curvilinear interaction on the text's cover.) Of most relevance to the members of SIG/MLR is the paucity of good applied interaction studies outside our journal. This is particularly disconcerting given the extensive discussion by numerous authors in Viewpoints. Upon the extensive discussion by numerous authors in viewpoints. Upon the early volumes of Viewpoints, we were astounded at the frequency and quality of interaction discussions. Desiring the work of these early "interactive pioneers" to not remain shelved, we will quote liberally.

Construction of interaction variables

An interaction variable is reflected in MLR as a product of two variables. If both variables are dichotomous then traditional ANOVA designs are being reflected. If one of the variables is dichotomous and the other continuous, then a difference between groups is being considered (evaluating "the question of homogeneous slopes [Jennings, 1972) or the difference between two correlation coefficients [Hoedt and Newman, 1984]). It has been shown that in the test for homogeneity of regression slopes, both methods of calculating analysis of covariance traditional ANCOVA and MLR — are exactly the same" (Newman and Fry 1972). (See also Jennings, 1972 and Williams, Naresh, and Peebles, 1972.)

If both of the variables are continuous then "continuous the "continuous then "continuous then "continuous then "continuous the "continuous then "continuous the "continuous then "continuous then "continuous then "continuo

If both of the variables are continuous then "continuous interaction" (McNeil and McNeil, 1975) or moderator variables are being investigated. Moderator variables "lend somewhat limited support for the use of more complex models. Moderators improve precition by acknowledging possible interactive effects of the moderator variable with other variables in the regression anlaysis. (Reed, Feldhusen, and Van

Modfrans, 1971)

If the variables are actually the same variable, then a higher order effect (curvilinearity) is being implemented. This extension of interaction into curvilinearity was first brought to the senior author's atttention by Jack Byrne during his Doctoral prelims. Dinero (1977) later makes the connection: Now that one has decided to use interaction terms in his prediction model, he has to decide which ones to include. The predictors raised to the first power, these variables squared or cubed or any of their cross-products may be used.

Dinero (1977) also reiterates the ease and value of conceptualizing

research within the MLR approach. "Once a researcher understands how to generate interactions, more avenues of investigation are open. The regression model brings with its flexibility a set of decisions many researchers in the past have either ignored or been unaware of."

Interpretation of interaction

Many researchers avoid interactions because of interpretation problems. Here is what Viewpoints authors have to say about the interpretation issue.

> "A significant interaction hampers the interpretation of main effects, but the positive view is that a significant F test of interaction tells us how to appropriately limit our generalization" (Spaner, 1977).

"A final word of warning is that second and higher order < interactions must be interpreted with great care, if meaningless or erroneous conclusions are not to be drawn from research data." (Brebner, 1972)

"In general, significant three-way interaction is seen to reflect different two-way interactions: if the ABC interaction is significantly different from zero, then either AB varies across C, AC varies across B, or BC varies across A. In any case, these differences would be manifest by significant cross-products of the standardized predictors. (Dinero, 1977)

*Indeed the value of need for interaction tests has been grossly underemphasized in MLR studies. I suspect that this phenomenon arises out of a misunderstanding, perhaps even fear. of a significant interaction finding." (Spaner, 1977) A MINNERS SECURIS AL

"Indeed the value of need for interaction tests has been grossly underemphasized in MLR studies. I suspect that this phenomenon arises out of a misunderstanding, perhaps even fear, of a significant interaction finding." (Spaner,

or berlynifes ers meldeinav eu McNeil and Beggs (1971) accepted the reality of interaction and challenged researchers to think about directional interactions — thus fully utilizing the power of their statistical test. No directional hypotheses have appeared in our review of Viewpoints.

Nonlinear predictors

"Since many of the simplest functional relationships in the physical sciences have been found to be non-linear or interactive, we find it interesting that few non-linear relationships have been established in the behavioral sciences, especially since most behavioral scientists would maintain that human behavior is no less complicated than physical behavior. " (McNeil, Evans, and McNeil, 1979)

There are "two reasons for including non-linear terms either the expected functional relationship is non-linear, or the way the construct has been originally measured needs to be modified." (McNeil, 1976)

"A more important situation occurs when there is theoretical or empirical justification for the inclusion of such a variable. (McNeil and Spaner, 1971)

Interpretation problems with non-linear terms have been addressed.

"When quadratic and interaction terms are significant, however, interpretation is made more difficult. Still, an attempt at interpretation seems somewhat better than ignoring the problem or assuming it does not exist."
(Reed, Feldhusen, and Van Modfrans, 1971)

"The range of manipulations available in order to test forms of curvilinearity is endless. However, contrived departure from linearity in regression models will not make trivial predictors into important ondes." (Jordan, 1971)

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Nonlinear criterion

There are two instances that come to mind when a nonlinear criterion would be used. One instance is when the functional relationship is indeed nonlinear (McNeil, Evans, and McNeil, 1979). The Pythagorean Theorem is one such example. Any criterion that is a ratio of one variable to another is another example. A second instance when a nonlinear criterion would be used is when the measure of the construct does not map the construct, and some rescaling of the measure is necessary (McNeil, et al 1979).

Potential problems

When continuous variables are multiplied to reflect the interaction term several potential problems must be avoided. One potential problem is that the product is dependent on the means and variances of the original scores. Thus, researchers might want to standardize the variables before obtaining the product (Dinero, 1977). McNeil and McNeil (1975) also discussed the scaling effect on the resultant R². The product of two continuous predictor variables may not accurately reflect the interaction. The precictor variables must be rescaled such that the product term does match the expectations of the criterion.

Miscellaneous techniques

The search for interaction in the hypothesis generating mode has been well stated by Dinero (1977).

"Given the problem of shrinkage, any regression anlaysis should be run in two phases, the first to estimate and the second to corroborate. This being the case, it may be just as wise to explore with the data of the first phase, to the extent of plotting the scatter diagrams, and use this information to select the interaction term to be used in the second phase. This type of exploration would seem to be almost a necessity in educational and phychological studies where there is little such comparative data available, where interaction has been something more to be avoided than awaited, and where complex aptitude-treatment interactions could bring exciting new interpretations to old data."

A computer program has been written to assist in finding the interactions which account for the most variance.

"The primary value of AID-4 to the task scientist is its ability to identify the maximum amount of variance in the criterion which can be accounted for by the predictors available; it relieves the task scientist of the trial-and-error task of attempting to identify the various relevant combinations of linear and non-linear interaction terms presently required by the multiple linear regression technique. The splitting process of AID-4, being based upon maximizing the between sums-of-squares and minimizing the within sums-of-squares, automatically takes all present interaction into account, indiciting the maximum variance predictable in the cirterion from the predictors." (Koplyay, 1972)

Finally, the dectection of interaction is one of the major advantages of the "regression model" in evaluating compensatory education programs (McNeil and Findlay, 1980). Discussion

The purpose for providing all the quotes in the previous sections was to document the interaction efforts made by authors in Viewpoints. The fact that the majority of these references are over 10 years old reflects more our concern for being aware of, and implementing existing methodology, rather than our lack of concern for improving existing

methodology.

Given that this methodology exists for studying interaction questions, why don't more researchers look at interaction? We don't have questions, why don't more researchers look at interaction? the answer, but we have some thoughts, and we will present them grouped

by the four major hypothesis testing steps.

with respect to literature review, most authors do not review interaction results, and when they do, they review them poorly. Furthermore, part of the publish or perish mentality is to invent new predictor variables, rather than try to increase the amount of variance accounted for. Finally, most researchers do not understand that different results from two studies implies an underlying interaction variable

In this world of posthoc orthogonal contrast coding and alpha protection levels few researchers realize that an interaction hypothesis can be specified all by itself, if no other question is of interest. But most of the statistics texts insist on a step-by-step procedure, looking at interaction in particular ways. What ever happened to the notion of

the research question guiding the statistical tool?

With respect to the actual testing of the hypothesis, we have three major concerns. First, canned ANOVA programs generally don't allow for testing specific interaction questions. Second, canned MLR programs encourage the inclusion of linear terms first. (Stepwise linear programs, though of value for some purposes, totally ignore the testing of a specific hypothesis.) Third, most statistics texts still present the interaction question as being valuable only for meeting assumptions - to reject so that main effects can be tested.

The fourth step in hypothesis testing, interpretation, also causes some problems for those considering interaction questions. Unfortunately most of our quoted Viewpoints authors acknowledge that interpreting an interaction result can be difficult. But if interaction is significant, then that is reflecting reality -- and shouldn't it be more valuable to make a "difficult" interpretation of reality as it is, than to make some make a "difficult" interpretation of reality as it is, than to make some make a "difficult" interpretation of reality. Perhaps researchers need to become more familiar with significant interaction.

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Summary Fortunately, for us, the summary of our paper was published in Viewpoints over 12 years ago.

"Perhaps one of the most overused assumptions within multivariate studies in educational research is that only simple linear relationships exist among the variables. Although interactive effects have been acknowledged within analysis of variance studies, the logical extension to regression analysis has rarely been actualized (Reed, Feldhusen, and Van Modfrans, 1971).

"Too often, even plausible interactions are ignored and all "Too often, even plausible interactions are ignored and all subjects are lumped together and, hence, treated as similar. Our conceptual theories have long ago turned to distinct groupings, and it is about time that our statistical procedures reflect this empirical possibility." (Newman, Lewis, and McNeil, 1973).

Unfortuanately these comments seem to still be appropriate today. Hopefully tomorrow they will not be appropriate.

Epilogue An examination of why interaction studies are not conducted in one specific area may shed some light on possible solutions. The two authors have been involved with educational program evaluations for several years. As such, we function as the program evaluator, providing evaluation information to the program manager. Traduction and the

In order to study an interaction question, the evaluator first needs to understand interaction concepts and be able to calculate interaction effects. Second, the evaluator must be able to translate these concepts into terms that the program manager can understand. Third, the interaction question must become of interest to the program manager, a person who often wants to use only the simplest of statements.

Collection of interaction information

Program managers usually want all students to be provided the best possible educatinal opportunity. This notion is usually envisioned in the same treatment for all. Denying treatments or parts of treatments is often not desired, and obtaining additional information from students is sometimes difficult if not impossible.

Verbal outcome

The program manager has a vested outcome in the program. Often the program has been devised by the manager and therefore the manager "knows" that the best program has been devised. Providing the same program to all students probably costs less, is easier administratively, and is usually more defensible to outside interests. The program manager is hard put to take the neutral stance towards the program that evaluators Implications if interaction is significant

First, the program evaluator must clearly communicate to the program manager the implications of a significant interaction. Then the program manager must incorporate this finding into next year's program, a task

which requires additional administrative attention.

When programs are constructed around significant interactions much additional administrative work is required. Program descriptions and guidelines must clearly reflect such interactions. Alternative programs must be delineated and procedures must be identified to get the right students (and probably the right teachers) into those programs. Different teaching materials may be required for the various programs, as well as different staff development. Classroom monitoring and program evaluations will continually need to incorporate those interactive variables. Consequently, additional administrative effort and commitment is required. Significant interactions imply that the KISS (Keep It Simple Stupid) principle is no longer applicable.

Roadblocks to replacing significant interactions

Everyone, including program managers, knows that results need to be replicated. The extent to which replicated results can be generalized to different settings and different students is usually an interesting question. But in the educational arena programs are often changed due to factors unrelated to evaluation results: a) new local, state, or Federal mandates, b) change in program manager, c) availability of personnel to plan and implement the program, and d) availability of funds.

Some possible next steps for SIG/MLR members

Now that we've a) established that adequate methodology exists to investigate interactive questions, b) documented that few interactive questions are being investigated, and c) specified some of the roadblocks to studying interactions in our field, we would like to propose some remediation.

First, we should all strive in our own daily endeavors to consider interaction hypotheses. We understand the methodology and can provide

exemplary behavior to other researchers.

Second, we could infuse other SIGs and the various AERA Divisions. We challenge each of you to become involved in another SIG, to spread the

interaction hypothesis.

Third, many of you participate in other national or regional educational meetings where more program managers are in attendance. These program people need to know that interaction questions can be tested - for behind every good program manager is an interaction hypothesis.

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If you are submitting a research article other than notes or comments, I would like to suggest that you use the following format if possible:

Title
Author and affiliation
Indented abstract (entire manuscript should be single spaced)
Introduction (purpose—short review of literature, etc.)
Method
Results
Discussion (conclusion)
References

All manuscripts should be sent to the editor at the above address. (All manuscripts should be camera-ready.)

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